Coupled Physical-Acoustical Data Assimilation in MAB/Shelfbreak PRIMER and First Comparison of the SCS and MAB Frontal Systems

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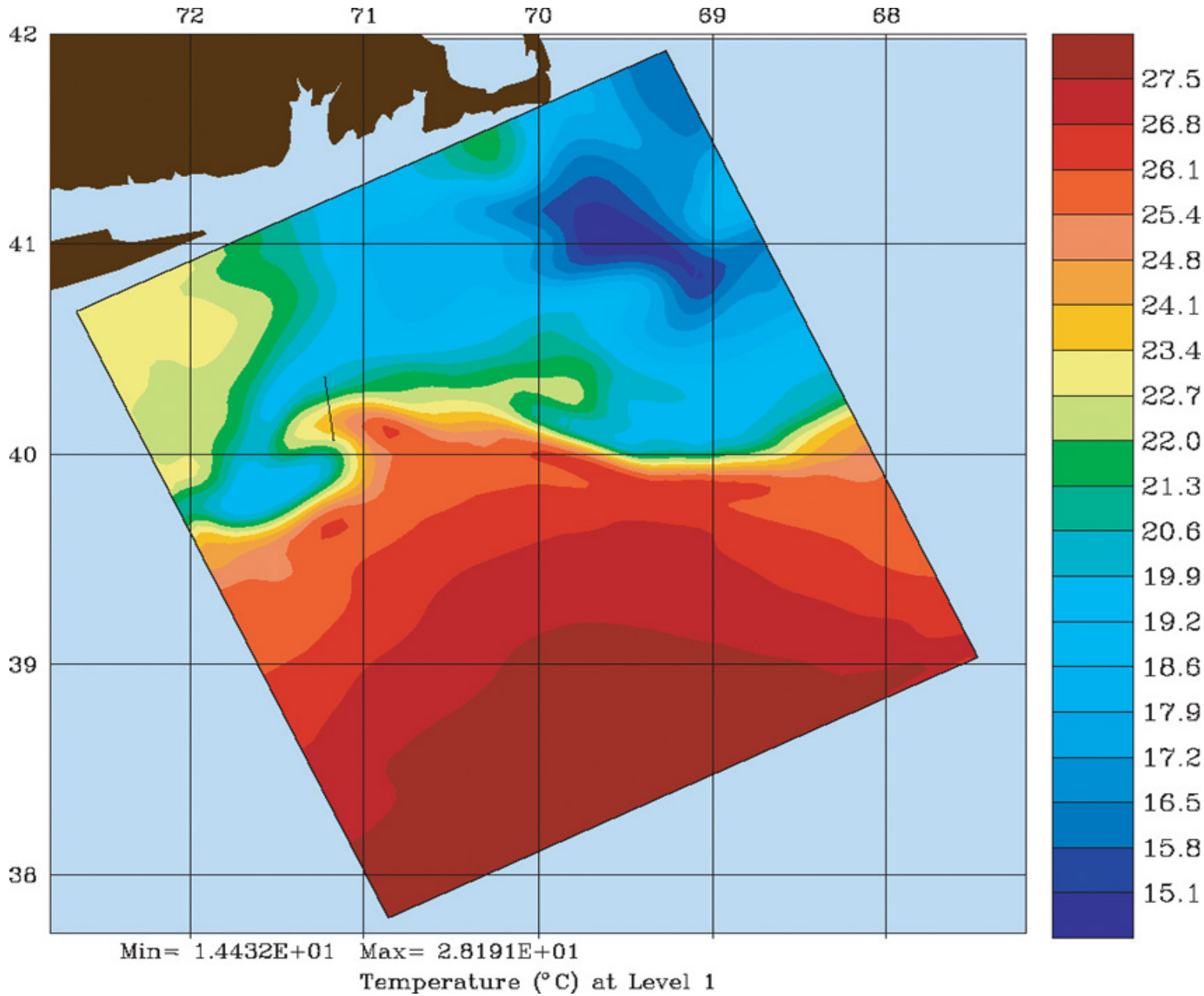
5. Conclusions

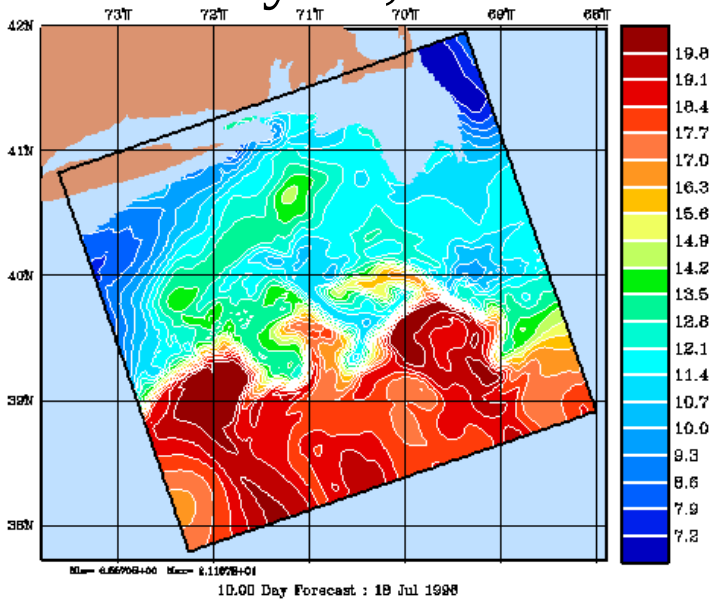
PHYSICAL-ACOUSTICAL FILTERING IN A SHELFBREAK ENVIRONMENT:

Ocean Physics as Simulated 2 Years Ago

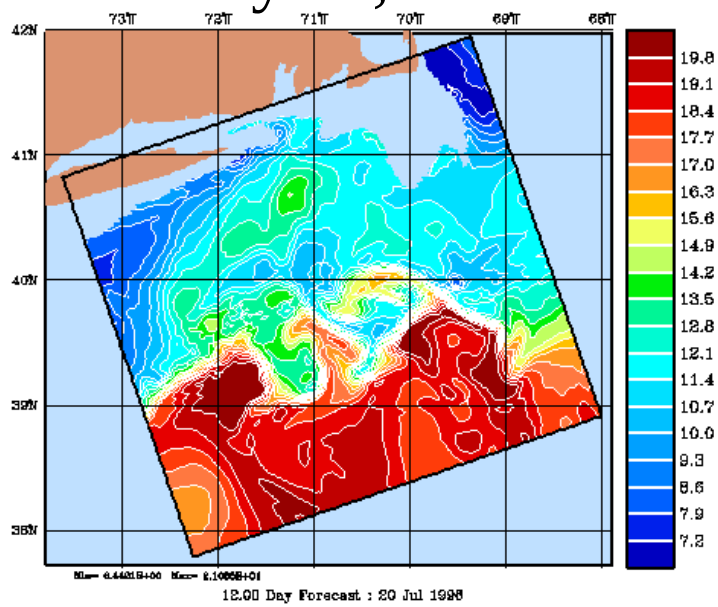


30m Temperature as Simulated in June 04

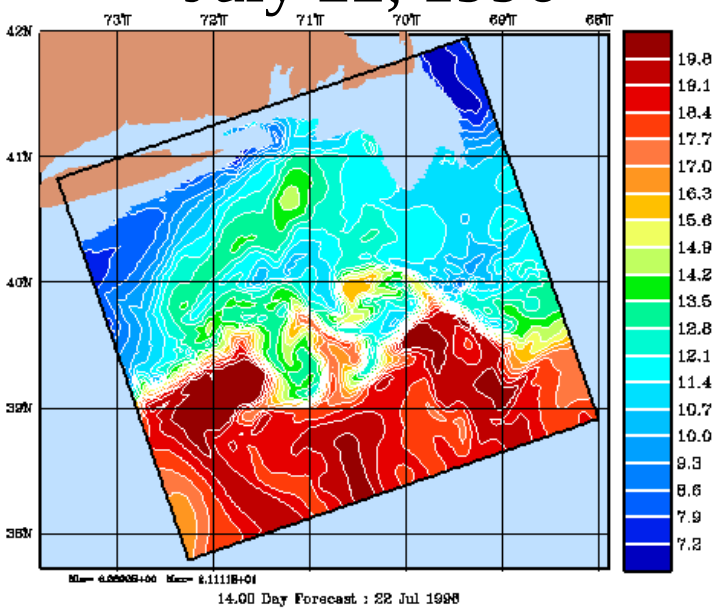
July 18, 1996



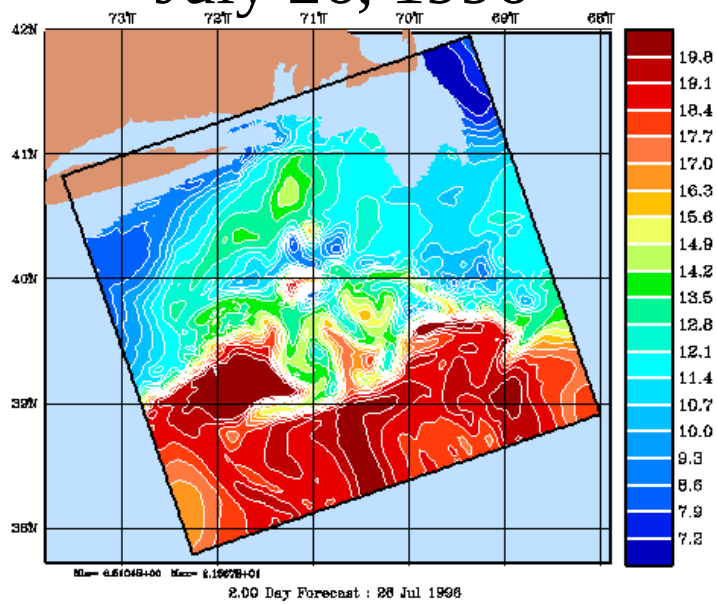
July 20, 1996



July 22, 1996

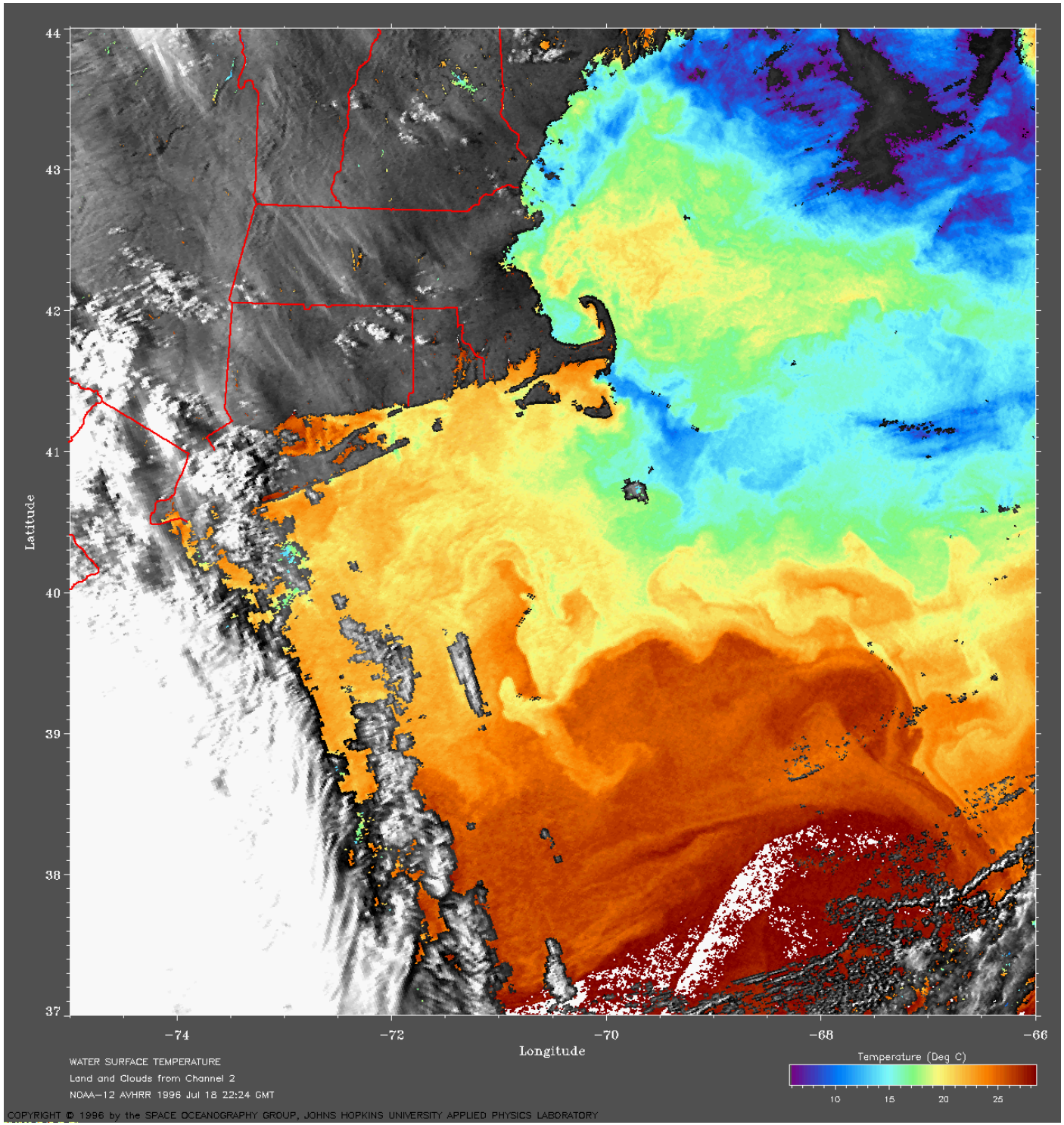


July 26, 1996



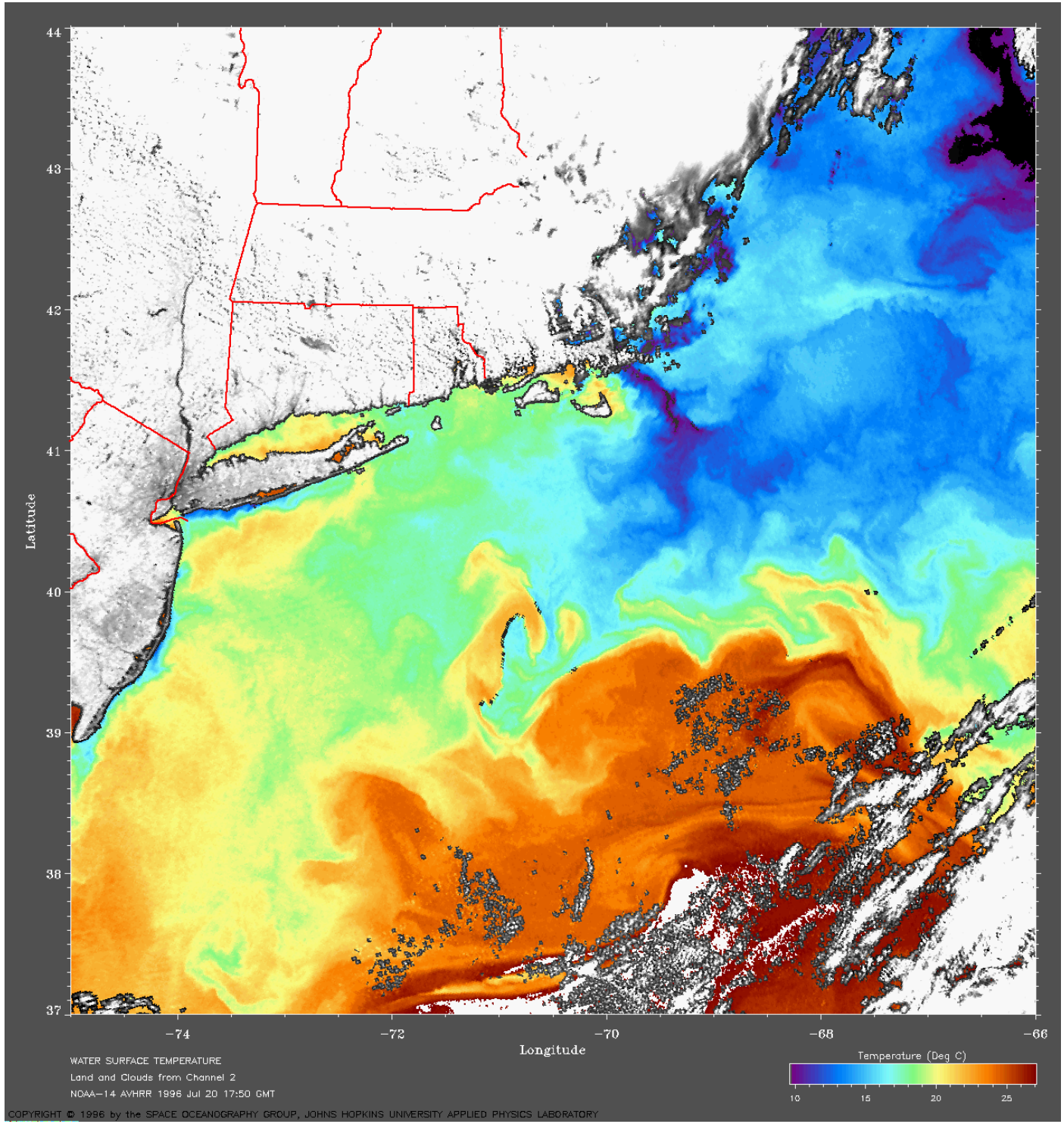
Evaluation based on SST

July 18



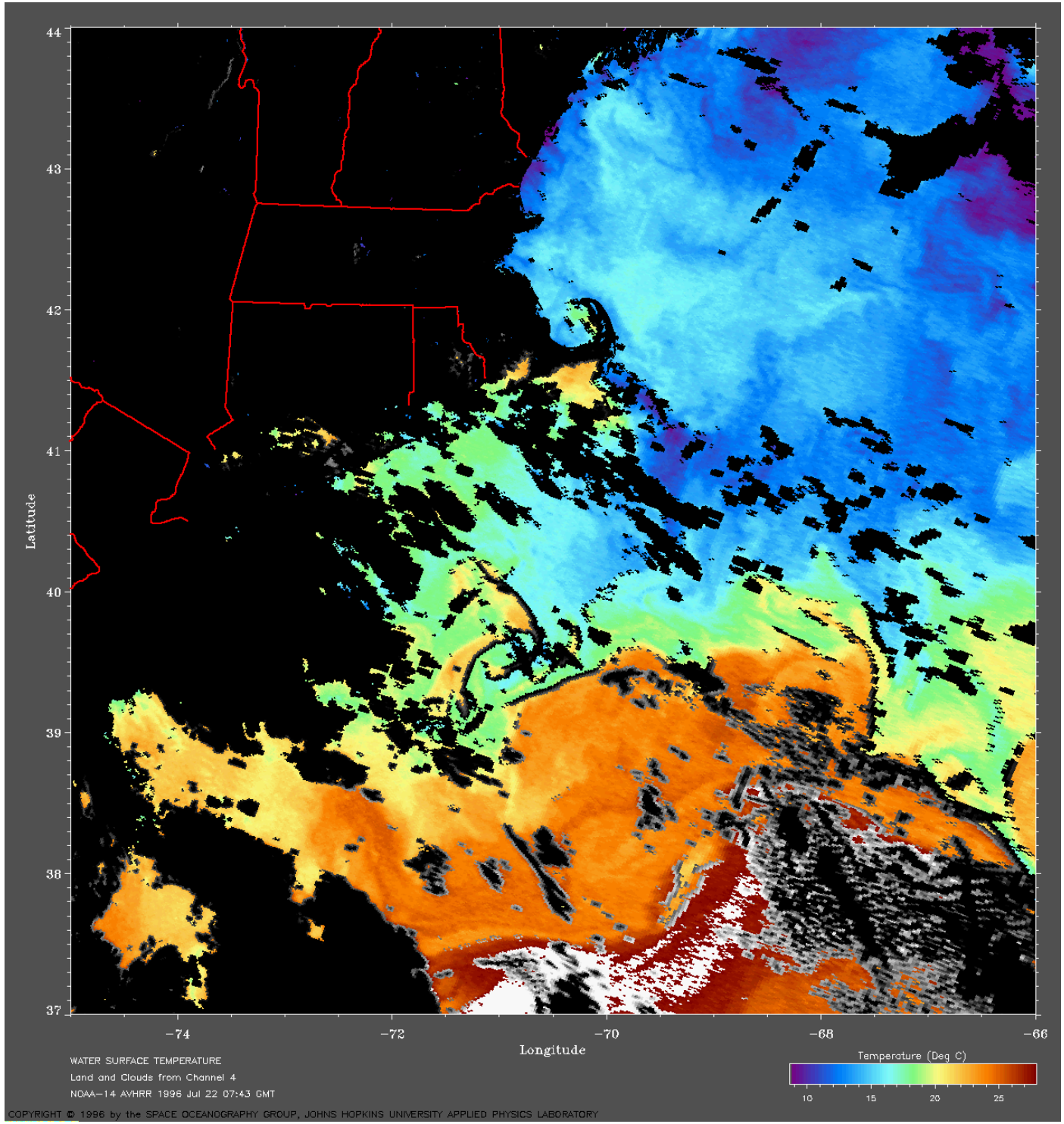
Evaluation based on SST

July 20

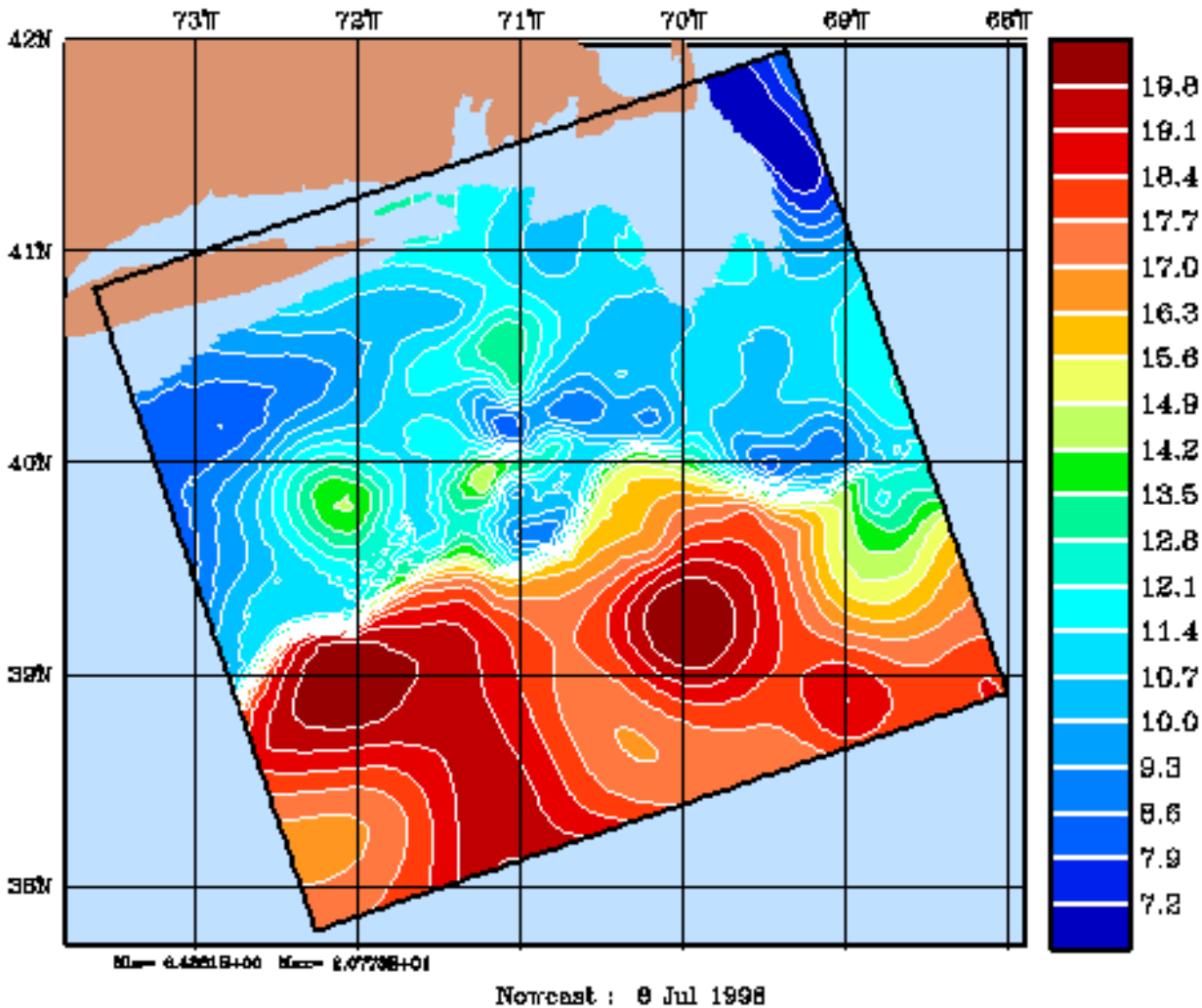


Evaluation based on SST

July 22

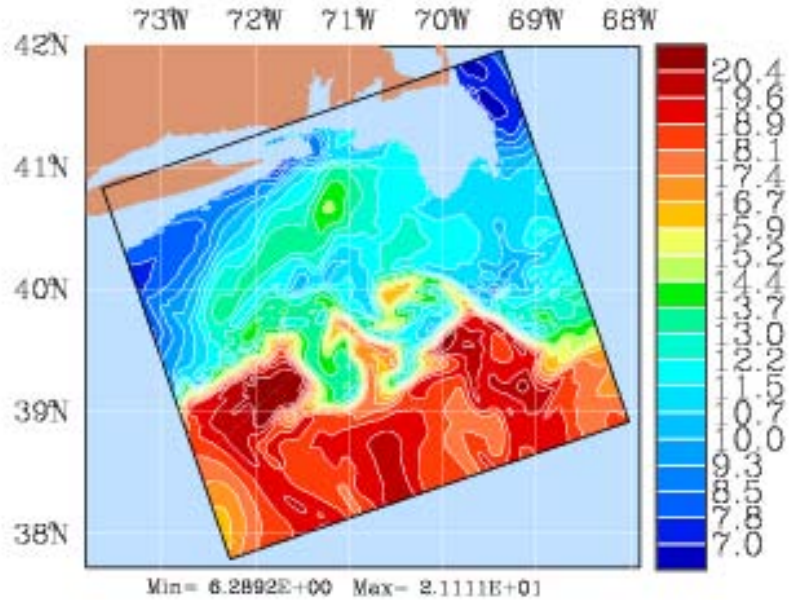


30m Temperature: 8 July – 7 August 1996

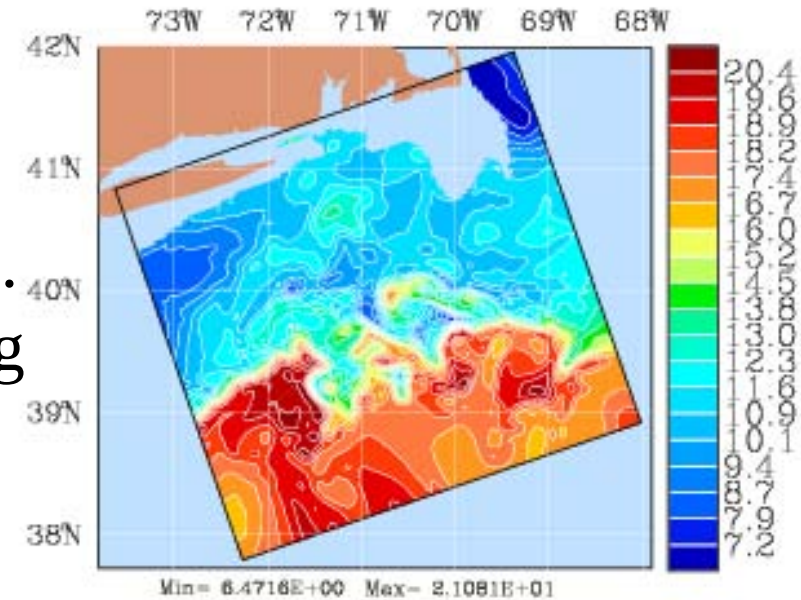


Importance and Effects of Atmospheric Forcings and Uncertainties

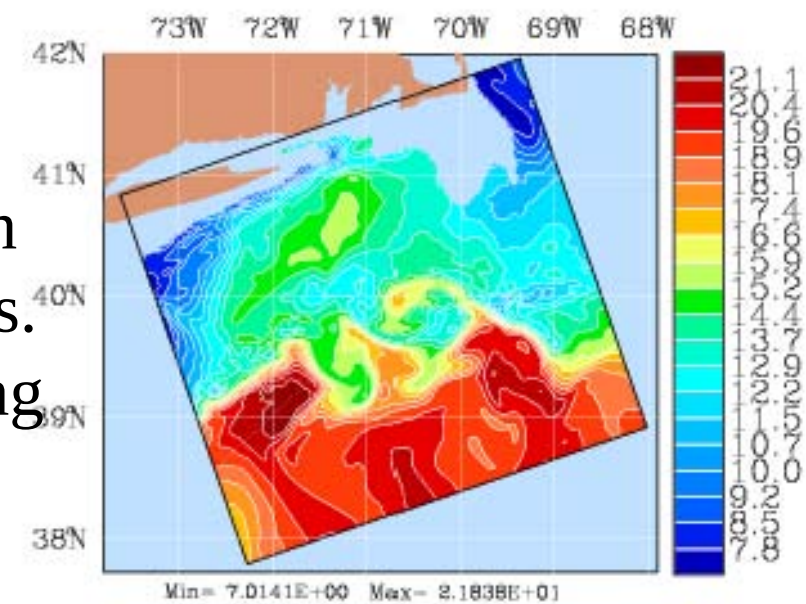
Best Run



No Atmos. Forcing



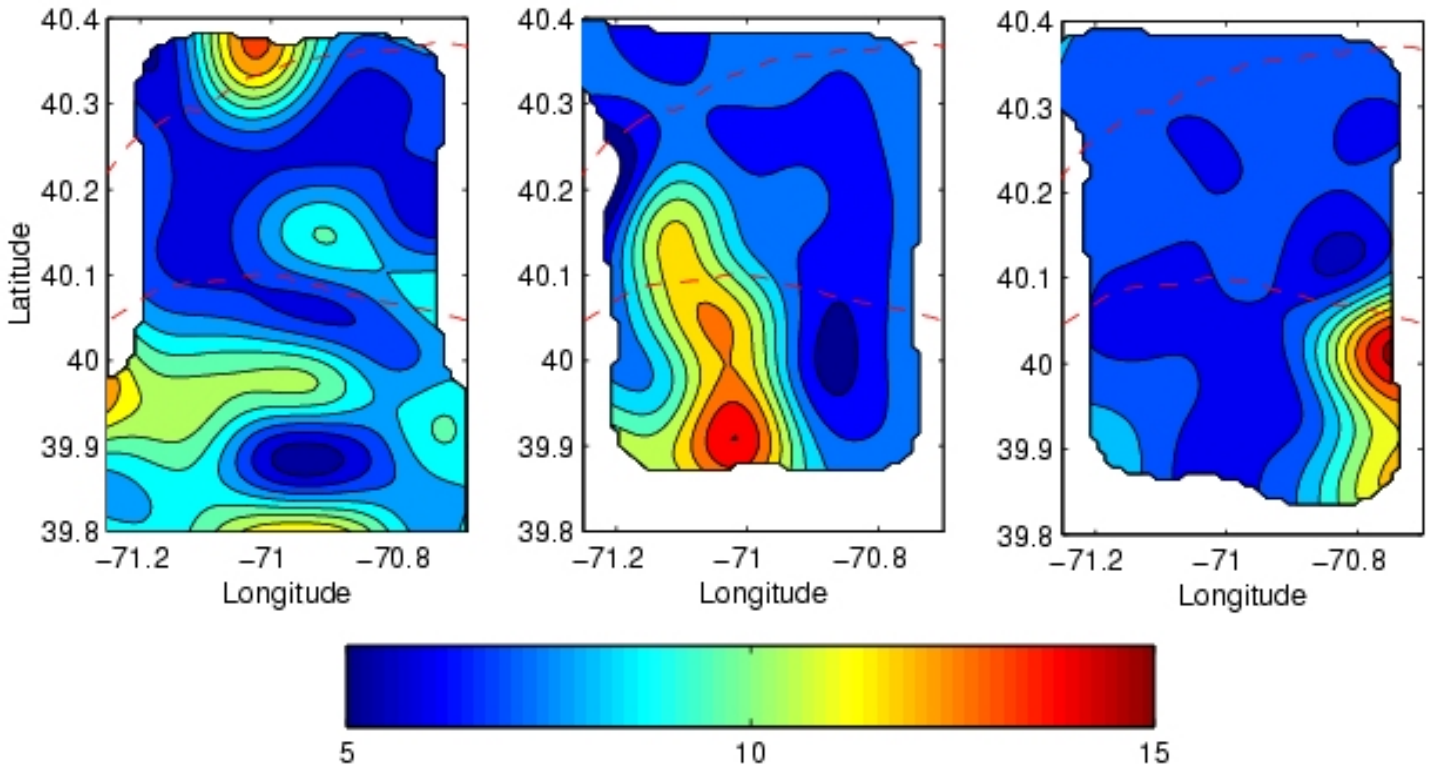
Too Much Atmos. Forcing



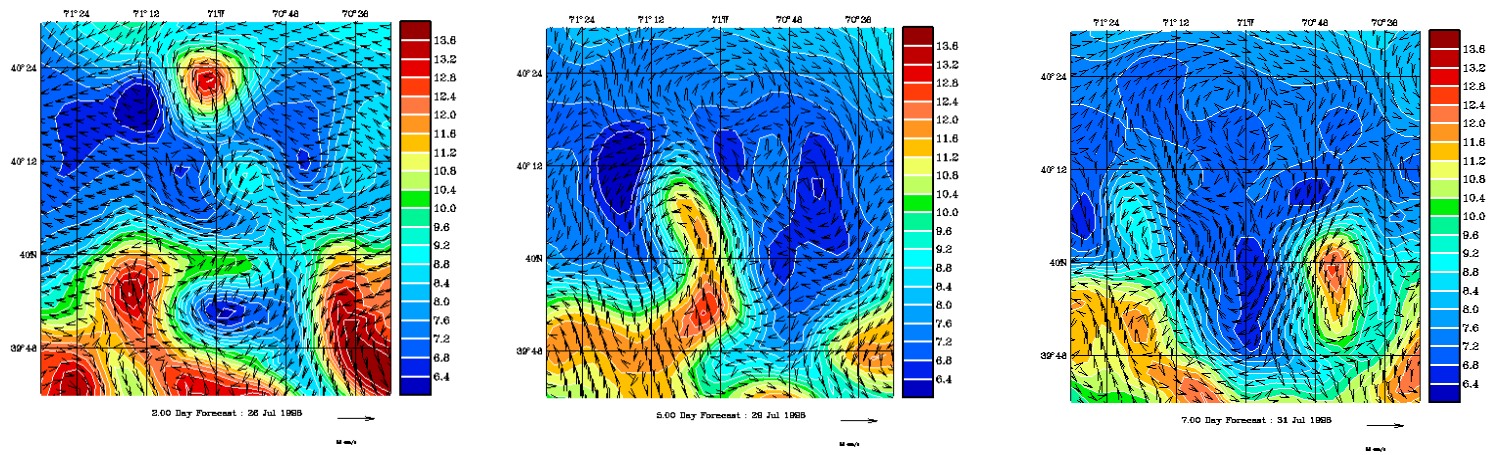
- Oceanic frontal instabilities from sub-mesoscales to mesoscales
- Atmospheric forcing impose certain scales on multi-scale oceanic frontal instability
- Increased atmos. forcing mixes large frontal meander at depth but does not lead to much stronger surface signal

Quick-Look evaluations of 50m Temperature: July 26, 1996

Gawarkiewicz, et al. 50m potential temperature for 26 July, 29 July and 31 July, objectively analyzed from Seasoar data

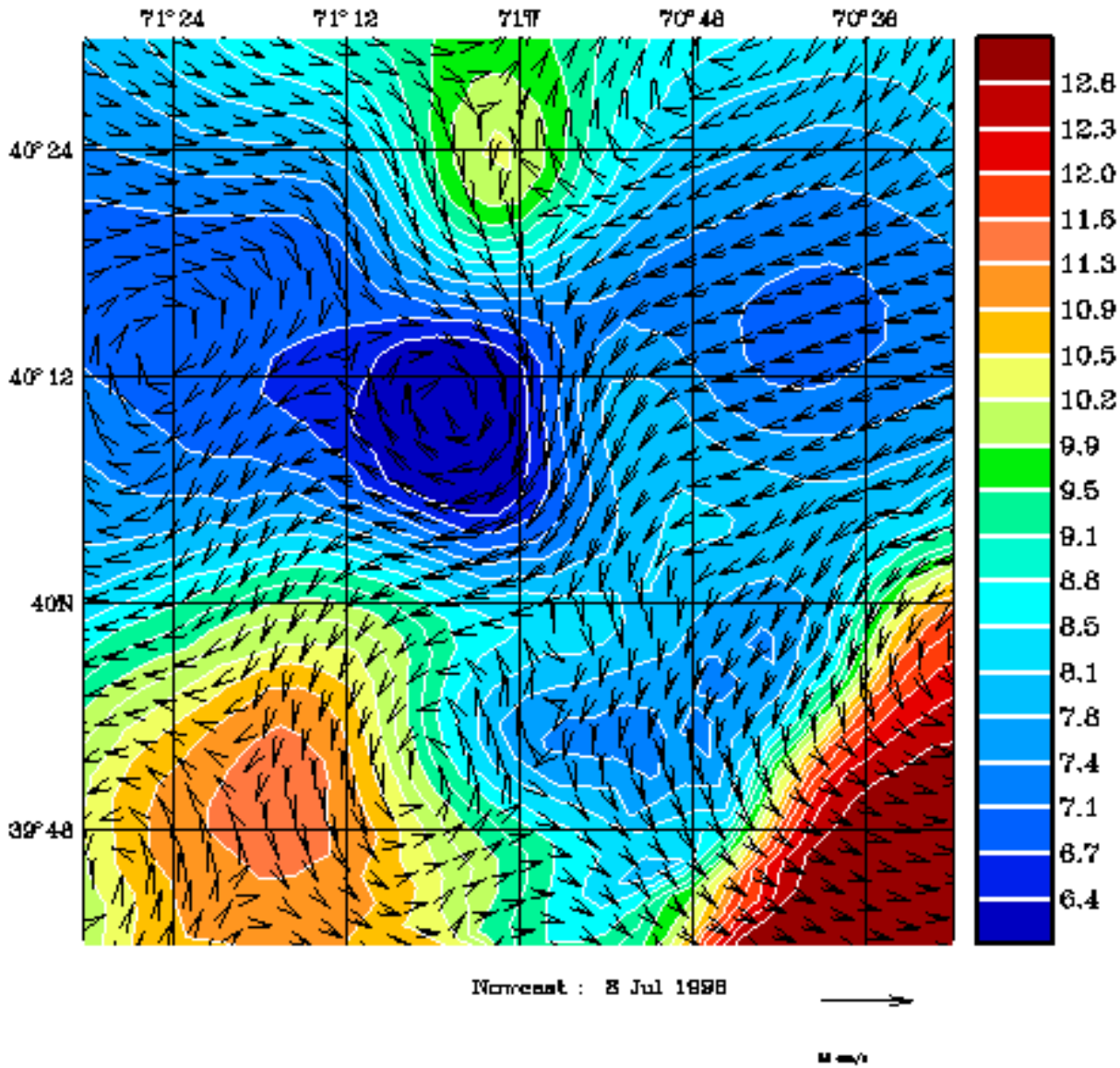


50m temperature in HOPS simulation with data assimilation for the same dates



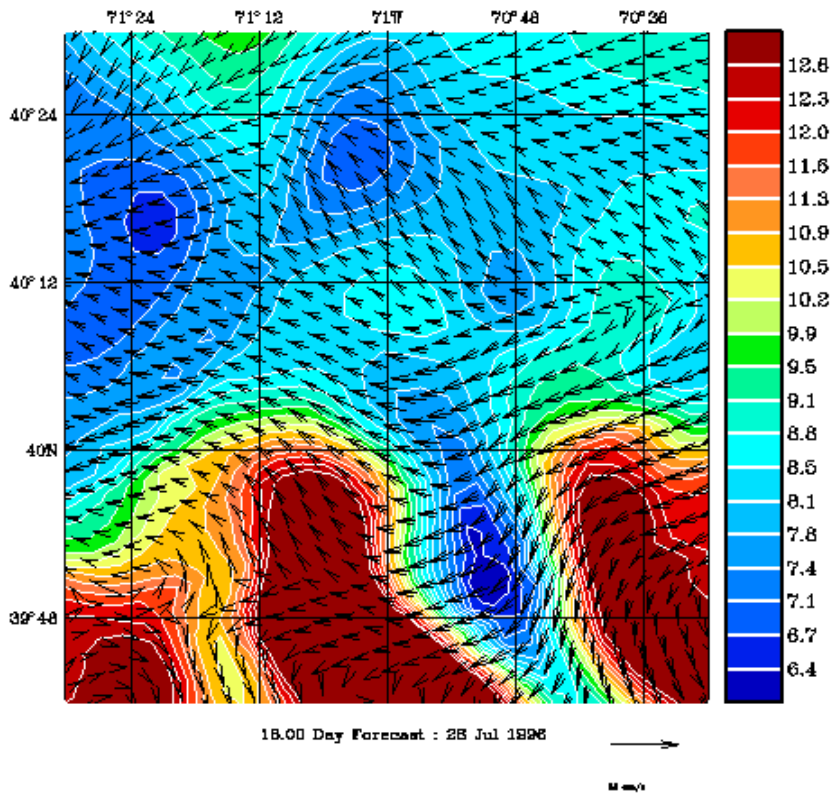
26 July 29 July 31 July

50m Temperature: 8 July – 7 August 1996



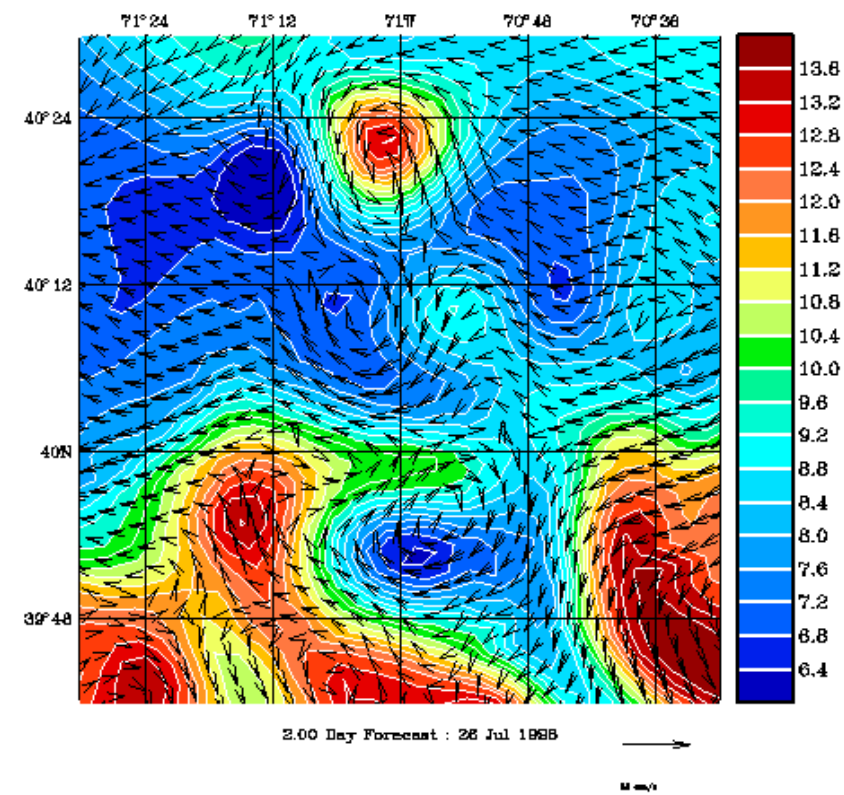
50m Temperature: July 26, 1996

No DA



18 day predictions

With DA



18 day predictions, with DA of July 26 data

ESSE: Uncertainty Predictions and Data Assimilation

1. Dynamics: $dx = M(x)dt + d\eta$ $\quad \eta \sim N(0, Q)$
2. Measurement: $y = H(x) + \varepsilon$ $\quad \varepsilon \sim N(0, R)$

3. Non-lin. Err. Cov. evolution: $P(0)=P_0$

$$dP/dt = <(x-\hat{x})(M(x)-M(\hat{x}))^T> + <(M(x)-M(\hat{x})(x-\hat{x})^T> + Q$$

4. Error reduction by DA:

$$P(+) = (I - KH)P(-)$$ where K is the reduced Kalman Gain

- ESSE retains and nonlinearly evolves uncertainties that matter, combining,

  i. Proper Orthogonal Decompositions (PODs) or Karhunen-Loeve (KL) expansions

  $$\mathbf{u} = \sum_{i=1}^{M} \phi_{\mathbf{u}}(x,y,z)\, \mathbf{a}_i(t) \quad \longrightarrow \quad \frac{d\,\mathbf{a}_i(t)}{dt} = \mathbf{f}(\mathbf{a})$$

  ii. Time-varying basis functions, and,

  iii. Multi-scale initialisation and Stochastic ensemble predictions

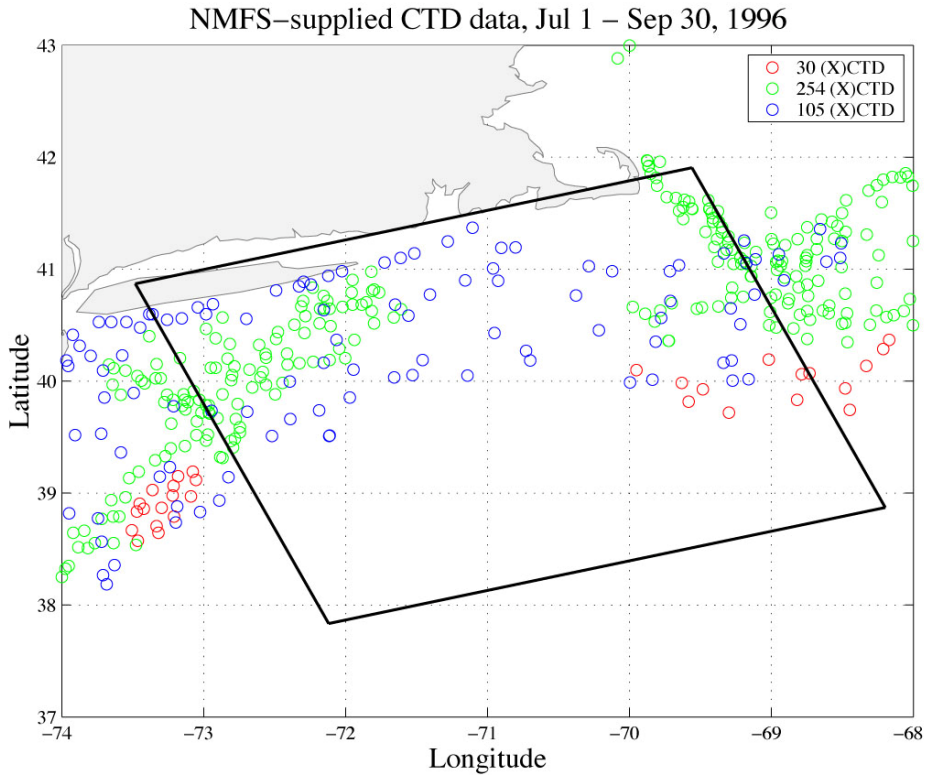
  to obtain a dynamic low-dimensional representation of the error space.

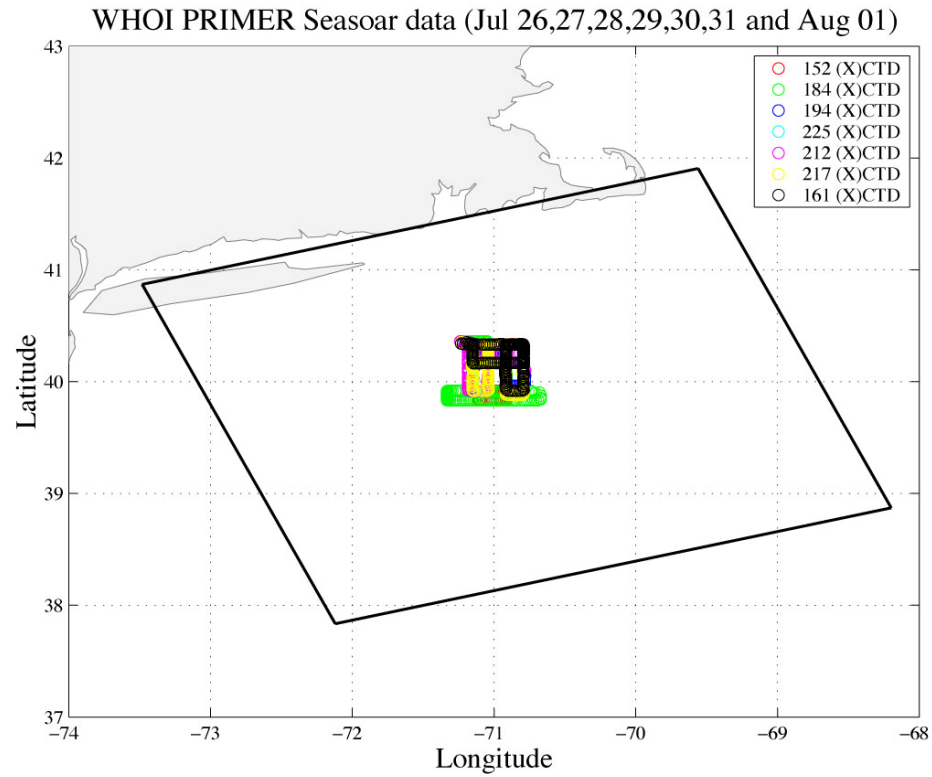
- Linked to Polynomial chaos, but with time-varying error KL basis:

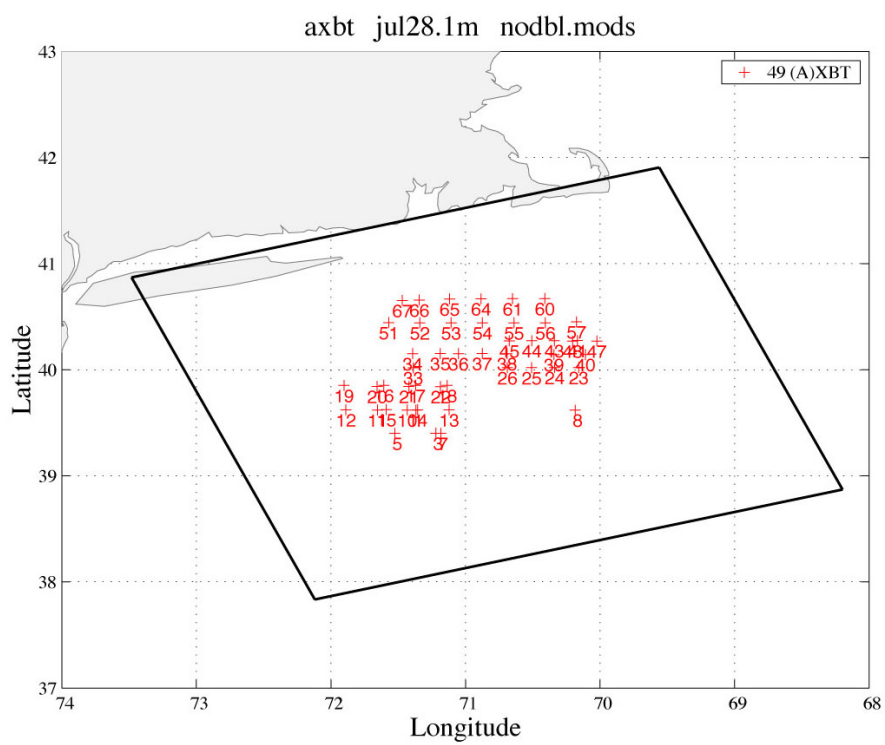
$$\mathbf{x}(x,t,\theta) = \bar{\mathbf{x}}(x,t) + \sum_{i=1}^{M} \sqrt{\lambda_i}\ \phi_u^s(\mathbf{x},t)\ \zeta_i(\theta)$$

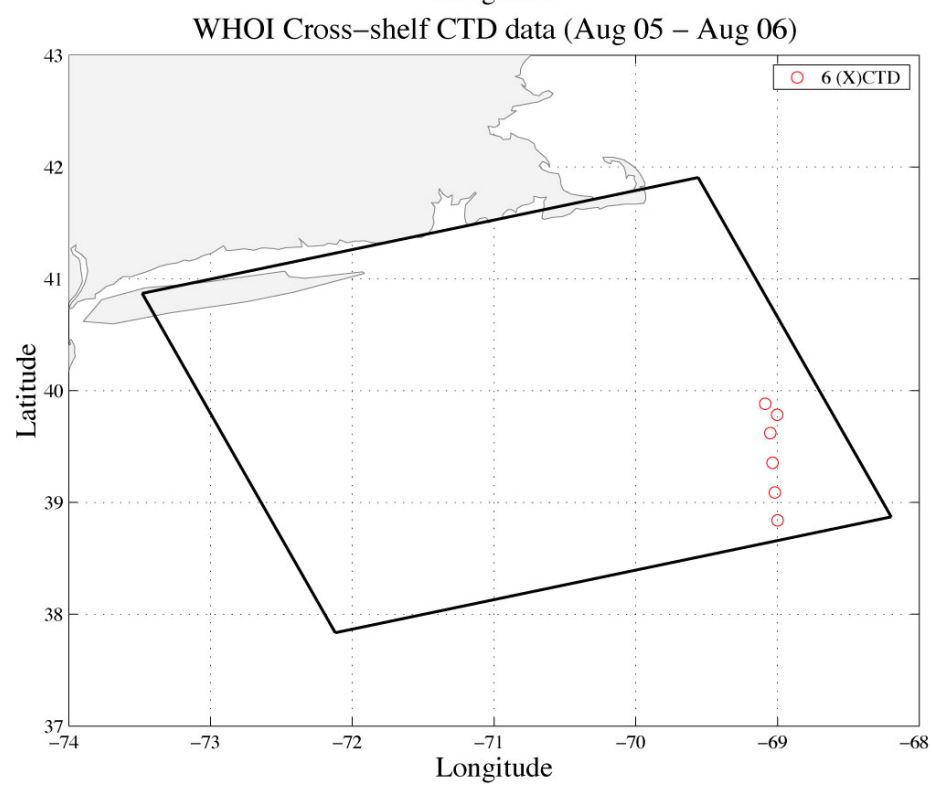
Sources of Uncertainty in Simulations of Ocean Physics

- Bathymetry
- Boundary conditions
  - Surface atmospheric forcing
  - Coastal-estuary and open-boundary fluxes
- Initial conditions
- Ocean physics data
- Model parameters and parameterized processes: sub-grid-scales, turbulence closures, un-resolved processes
  - e.g. tides and internal tides, internal waves and solitons, microstructure and turbulence
- Numerical errors: steep topographies/pressure gradient, non-convergence

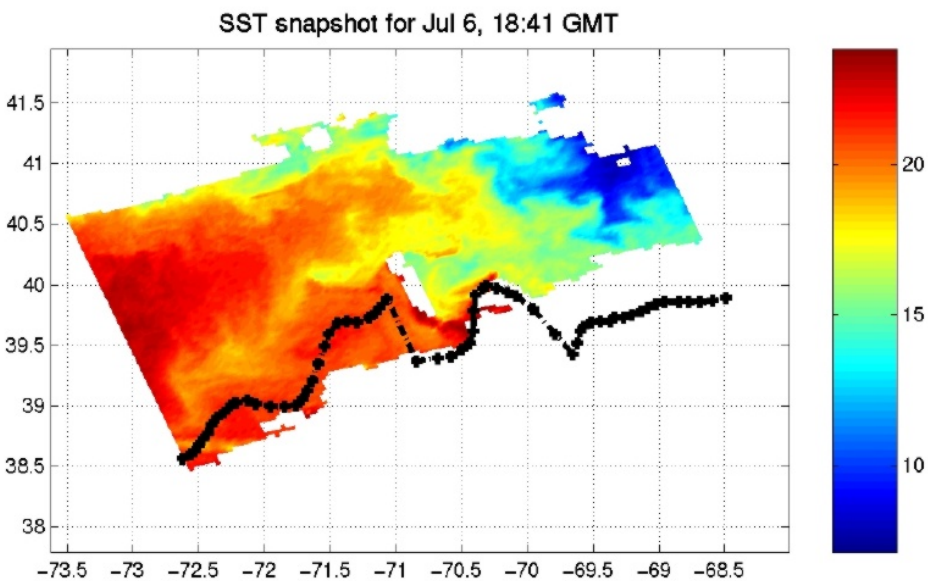

NMFS−supplied CTD data, Jul 1 − Sep 30, 1996
30 (X)CTD
254 (X)CTD
105 (X)CTD
Latitude
Longitude

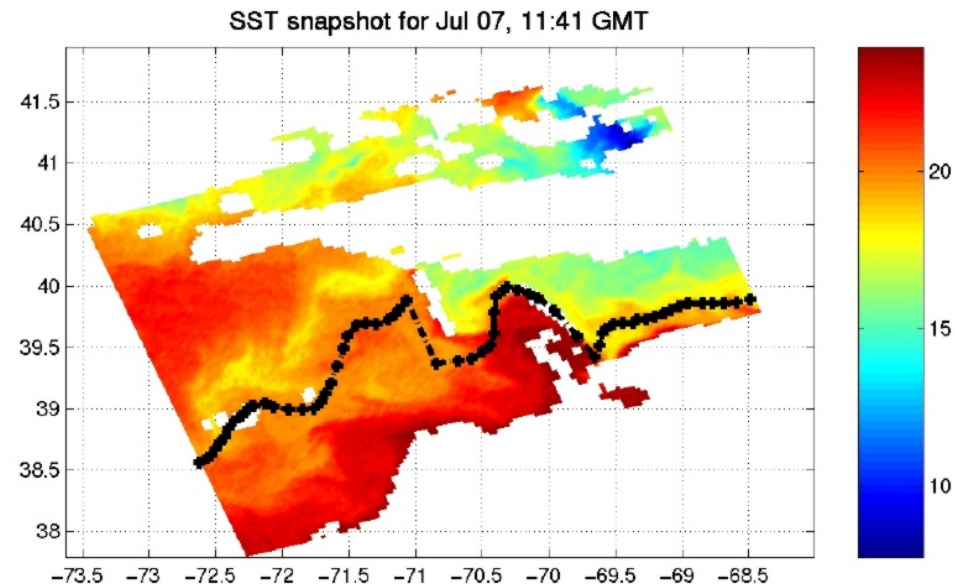

WHOI PRIMER Seasoar data (Jul 26,27,28,29,30,31 and Aug 01)
152 (X)CTD
184 (X)CTD
194 (X)CTD
225 (X)CTD
212 (X)CTD
217 (X)CTD
161 (X)CTD
Latitude
Longitude

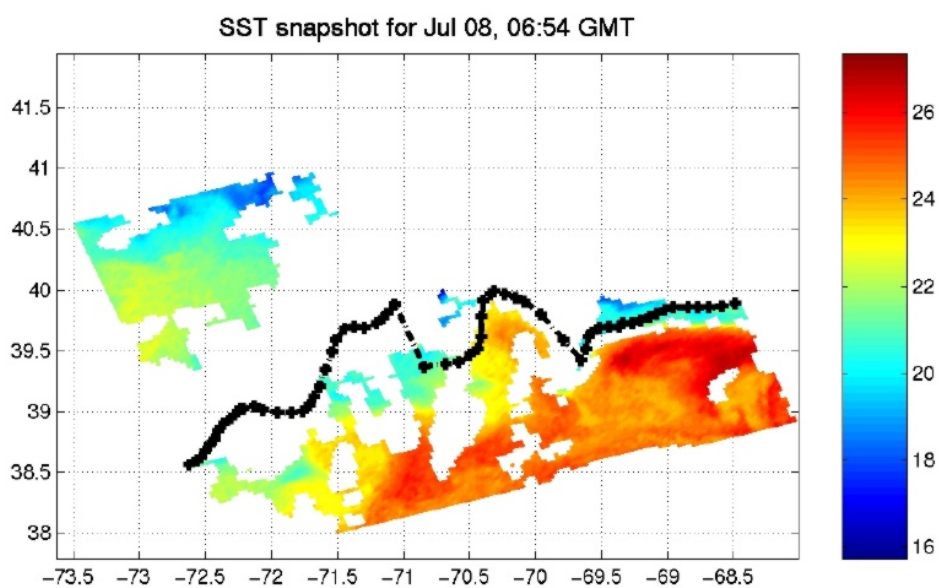

axbt jul28.1m nodbl.mods
49 (A)XBT
Latitude
Longitude


WHOI Cross−shelf CTD data (Aug 05 − Aug 06)
6 (X)CTD
Latitude
Longitude

Initial condition uncertainties: Positions and shapes of the tilted shelfbreak front



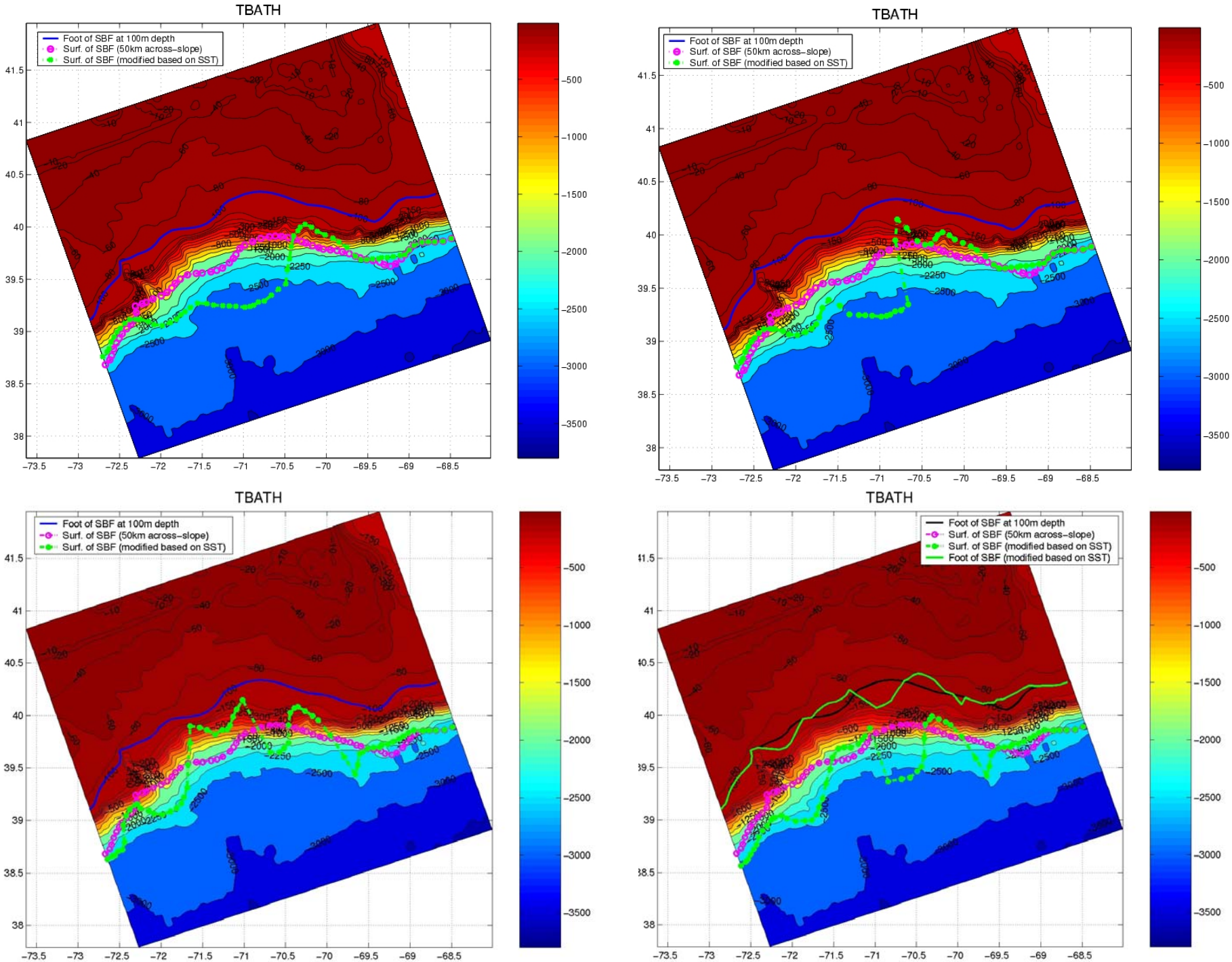




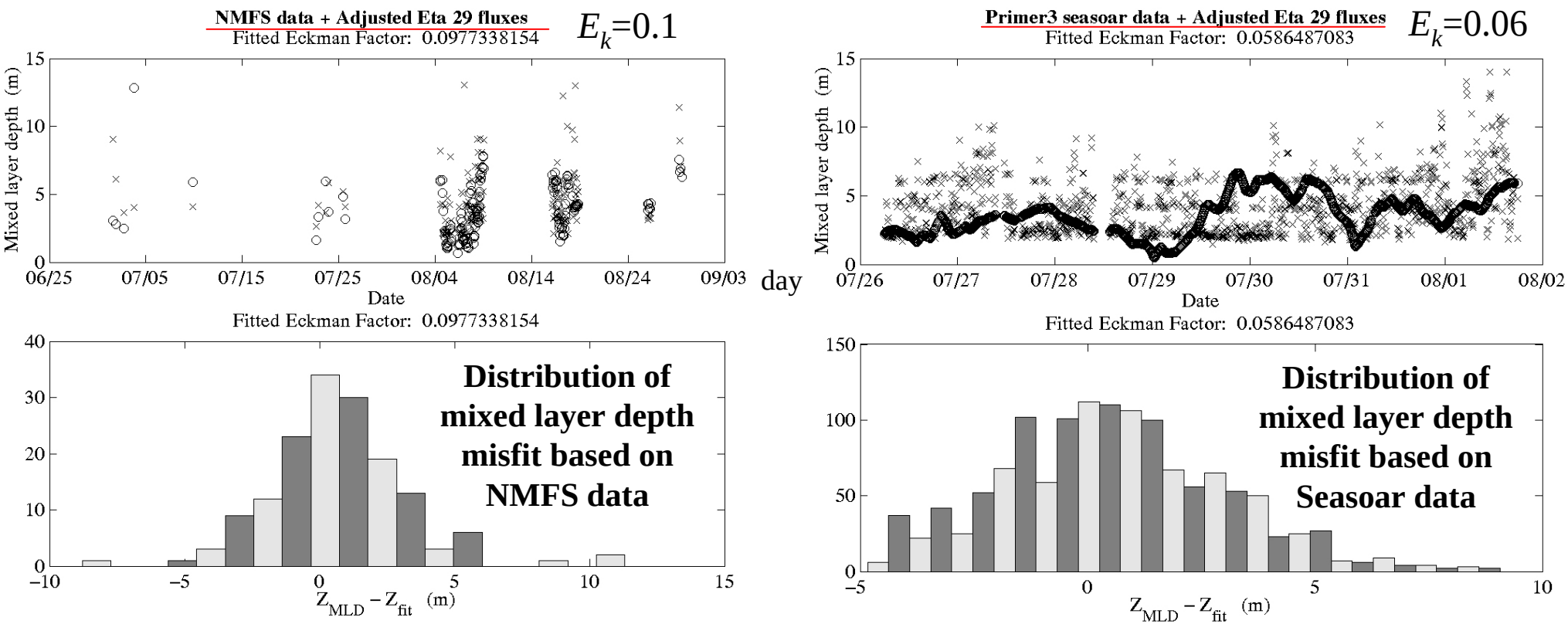
Outcropping of surface front

- Upstream positions relatively certain, with sharp ring-front interactions
- Downstream positions very uncertain:
  - Notice surface signature of advected shelf waters
  - SBF meandering and “old” weak warm core rings
  - Squirts of slope and shelf waters

IC uncertainties: Positions and shapes of the tilted SBF (cont.)



Uncertainties in Multiple Model Parameters: Example of mixing layer depth (Ekman factor E_k)



- Similar uncertainties and fit for several other parameters
- Need for adaptive modeling (e.g. parameter values that evolve in time as a function of data)
- One reason: (sub)-mesocale coastal variabilities and atmosphere-ocean interactions are not stationary at scales of days to a month

Stochastic Primitive Equation Model

The diagonal of time-decorrelations:

$\boldsymbol{\beta}_u$, $\boldsymbol{\beta}_v$, $\boldsymbol{\beta}_T$, $\boldsymbol{\beta}_S$, $\boldsymbol{\beta}_\psi$ **functions of** (x, y, z)

are here chosen $\boldsymbol{\beta}_X = \beta \mathbf{I}$.

The diagonal of noise variances are chosen function of z **only, of amplitude set to:**
"ε * geostrophy"

$$\boldsymbol{\Sigma}_u = \boldsymbol{\Sigma}_v = \sigma^2(z)\,\mathbf{I}\ , \quad \text{with } \sigma_U(z) = \epsilon_U\, f_c\, U(z)\ ,$$

$$\boldsymbol{\Sigma}_T = \sigma_T^2(z)\,\mathbf{I}\ , \quad \text{with } \sigma_T(z) = \epsilon_T\, U(z)\, \frac{\Delta T(z)}{L(z)}\ ,$$

$$\boldsymbol{\Sigma}_S = \sigma_S^2(z)\,\mathbf{I}\ , \quad \text{with } \sigma_S(z) = \epsilon_S\, U(z)\, \frac{\Delta S(z)}{L(z)}\ ,$$

$$\boldsymbol{\Sigma}_\psi = \sigma_\psi^2(z)\,\mathbf{I}\ , \quad \text{with } \sigma_\psi(z) = \epsilon_\psi\, \frac{\overline{\omega}\, L(z)}{U(z)}\ ,$$

Internal Baroclinic Zonal Mode

$$\mathbf{d\hat{u}} = \mathbf{du}' - \mathbf{d\overline{u}}'\ , \tag{82a}$$

$$\mathbf{du}' = \left(-\boldsymbol{\Gamma}(\mathbf{u}) + \mathbf{fv} - \frac{\mathbf{g}}{\boldsymbol{\rho}_0}\int_{\mathbf{z}}^{0} \boldsymbol{\rho}_{\mathbf{x}}\, \mathbf{dz} + \mathbf{F}_u + \mathbf{A}_v \mathbf{u}_{\mathbf{zz}}\right) dt + \mathbf{B}_u^{fc}\, \mathbf{d\tilde{w}}_u^c\ ,$$

$$\text{with}\quad \mathbf{u} = \mathbf{\hat{u}} - \frac{1}{\mathbf{H}}\boldsymbol{\psi}_{\mathbf{y}}\ .$$

$$\mathbf{d\tilde{w}}_u^c = -\boldsymbol{\beta}_u\, \mathbf{\tilde{w}}_u^c\, dt + \mathbf{dw}_u^c\ , \tag{82b}$$

$$\text{with}\quad \mathbf{\tilde{w}}_u^c(0) \sim (\mathbf{0}, \boldsymbol{\Sigma}_u)\quad \text{and}\quad \mathbf{w}_u^c \sim (\mathbf{0}, 2\boldsymbol{\beta}_u \boldsymbol{\Sigma}_u)\ .$$

Internal Baroclinic Meridional Mode

$$\mathbf{d\hat{v}} = \mathbf{dv}' - \mathbf{d\overline{v}}'\ , \tag{82c}$$

$$\mathbf{dv}_t' = \left(-\boldsymbol{\Gamma}(\mathbf{v}) - \mathbf{fu} - \frac{\mathbf{g}}{\boldsymbol{\rho}_0}\int_{\mathbf{z}}^{0} \boldsymbol{\rho}_y\, \mathbf{dz} + \mathbf{F}_v + \mathbf{A}_v \mathbf{v}_{\mathbf{zz}}\right) dt + \mathbf{B}_v^{fc}\, \mathbf{d\tilde{w}}_v^c\ ,$$

$$\text{with}\quad \mathbf{v} = \mathbf{\hat{v}} + \frac{1}{\mathbf{H}}\boldsymbol{\psi}_{\mathbf{x}}\ .$$

$$\mathbf{d\tilde{w}}_v^c = -\boldsymbol{\beta}_v\, \mathbf{\tilde{w}}_v^c\, dt + \mathbf{dw}_v^c\ , \tag{82d}$$

$$\text{with}\quad \mathbf{\tilde{w}}_v^c(0) \sim (\mathbf{0}, \boldsymbol{\Sigma}_v)\quad \text{and}\quad \mathbf{w}_v^c \sim (\mathbf{0}, 2\boldsymbol{\beta}_v \boldsymbol{\Sigma}_v)\ .$$

Thermal energy: Balance

$$\mathbf{dT} = \left(-\boldsymbol{\Gamma}(\mathbf{T}) + \mathbf{F}_T + \mathbf{K}_v \mathbf{T}_{\mathbf{zz}}\right) dt + \mathbf{B}_T^{fc}\, \mathbf{d\tilde{w}}_T^c\ , \tag{82e}$$

$$\mathbf{d\tilde{w}}_T^c = -\boldsymbol{\beta}_T\, \mathbf{\tilde{w}}_T^c\, dt + \mathbf{dw}_T^c\ , \tag{82f}$$

$$\text{with}\quad \mathbf{\tilde{w}}_T^c(0) \sim (\mathbf{0}, \boldsymbol{\Sigma}_T)\quad \text{and}\quad \mathbf{w}_T^c \sim (\mathbf{0}, 2\boldsymbol{\beta}_T \boldsymbol{\Sigma}_T)\ .$$

Conservation : of Salt

$$\mathbf{dS} = \left(-\boldsymbol{\Gamma}(\mathbf{S}) + \mathbf{F}_S + \mathbf{K}_v \mathbf{S}_{\mathbf{zz}}\right) dt + \mathbf{B}_S^{fc}\, \mathbf{d\tilde{w}}_S^c\ , \tag{82g}$$

$$\mathbf{d\tilde{w}}_S^c = -\boldsymbol{\beta}_S\, \mathbf{\tilde{w}}_S^c\, dt + \mathbf{dw}_S^c\ , \tag{82h}$$

$$\text{with}\quad \mathbf{\tilde{w}}_S^c(0) \sim (\mathbf{0}, \boldsymbol{\Sigma}_S)\quad \text{and}\quad \mathbf{w}_\psi^c \sim (\mathbf{0}, 2\boldsymbol{\beta}_\psi \boldsymbol{\Sigma}_S)\ .$$

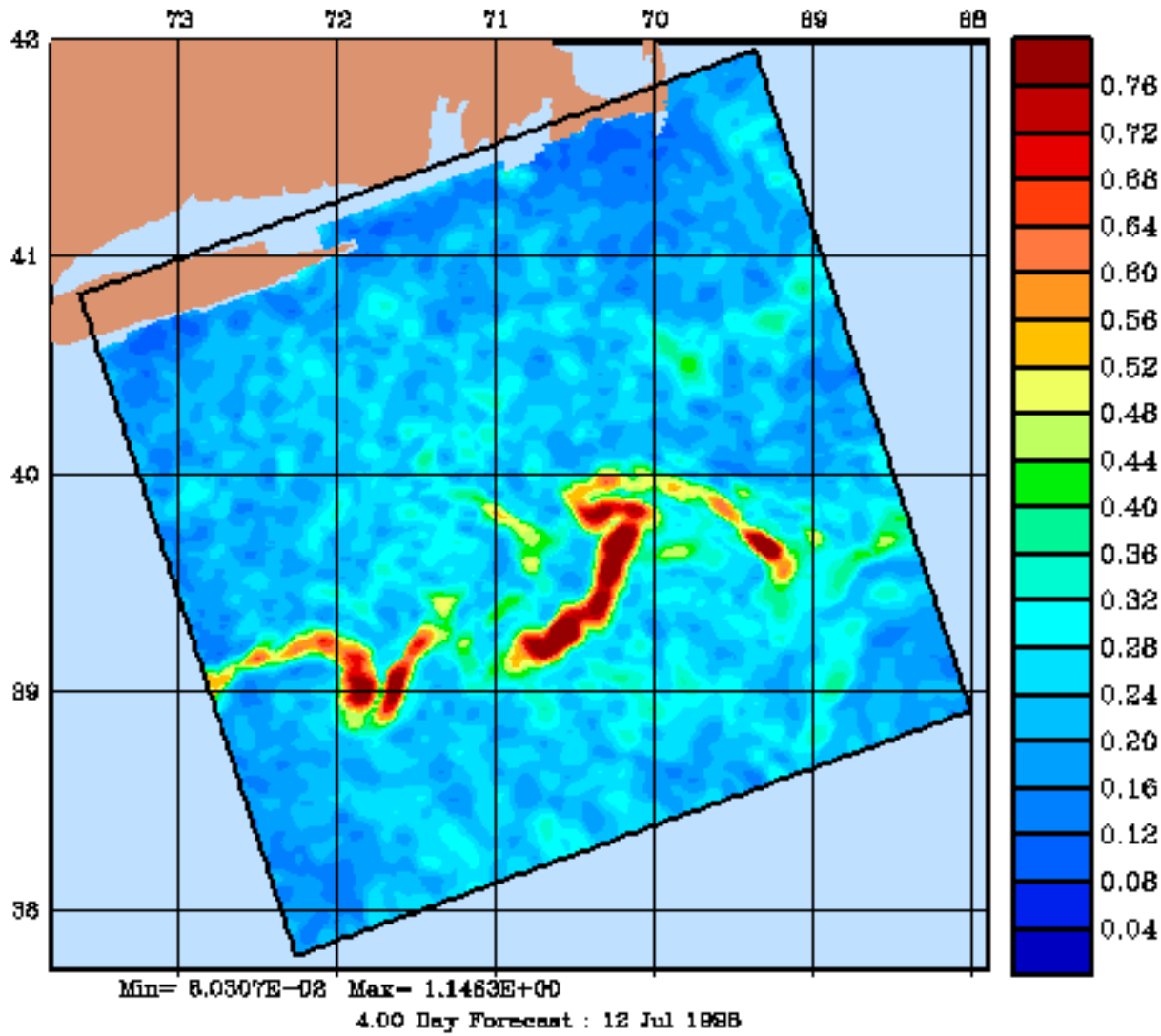
Barotropic Stream Function

$$\nabla_h \wedge [\mathbf{H}^{-1}\nabla_{\mathbf{h}} \wedge \mathbf{d}\boldsymbol{\psi}\, \mathbf{e}_3] = -\nabla_h \wedge \mathbf{d\overline{u}} + \mathbf{B}_\psi^{fc}\, \mathbf{d\tilde{w}}_\psi^c\ , \tag{82i}$$

$$\mathbf{d\tilde{w}}_\psi^c = -\boldsymbol{\beta}_\psi\, \mathbf{\tilde{w}}_\psi^c\, dt + \mathbf{dw}_\psi^c\ . \tag{82j}$$

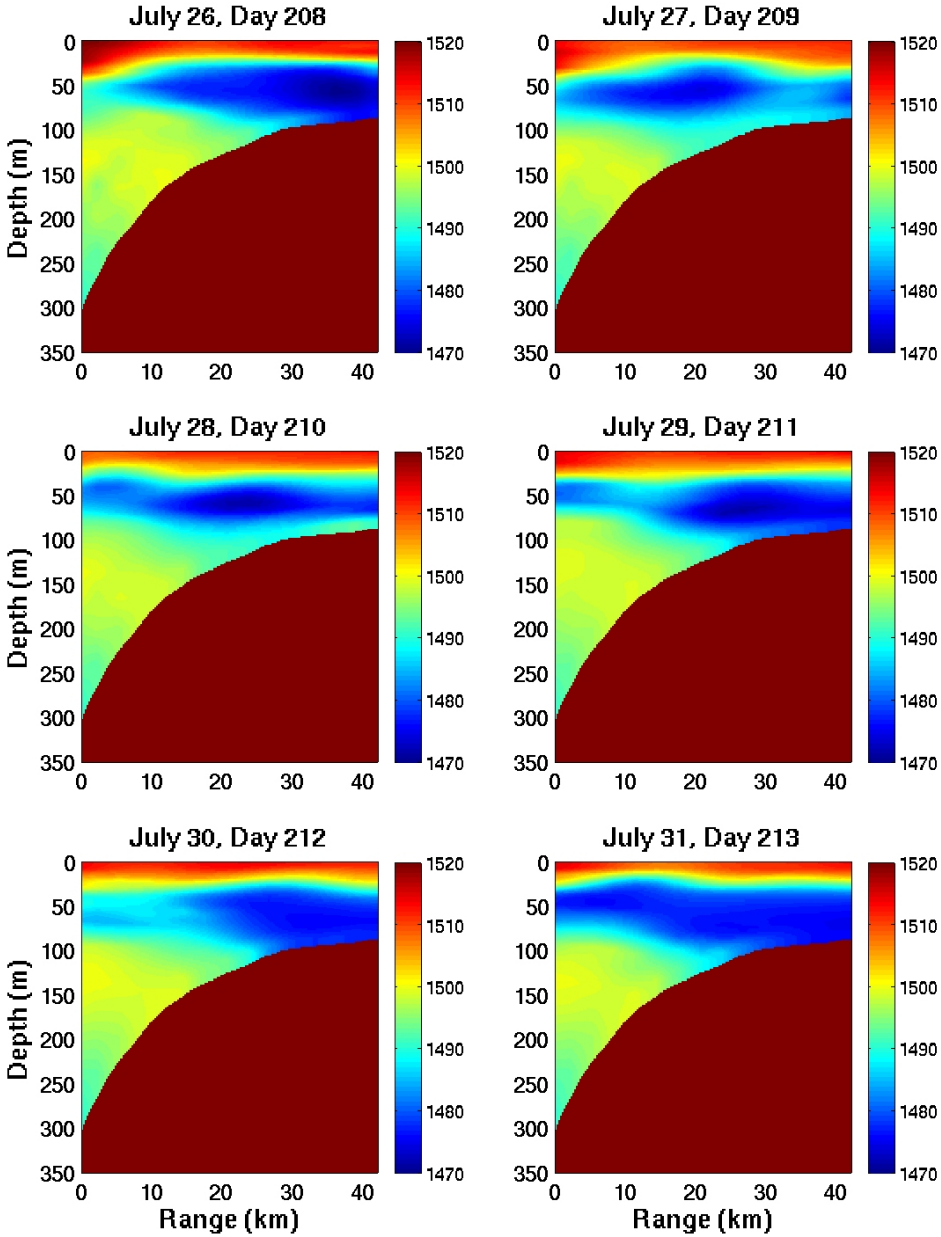
$$\text{with}\quad \mathbf{\tilde{w}}_\psi^c(0) \sim (\mathbf{0}, \boldsymbol{\Sigma}_\psi)\quad \text{and}\quad \mathbf{w}_\psi^c \sim (\mathbf{0}, 2\boldsymbol{\beta}_\psi \boldsymbol{\Sigma}_\psi)\ .$$

Evolution of Uncertainties:
Predicted Standard Deviation of Temperature Error at 10m

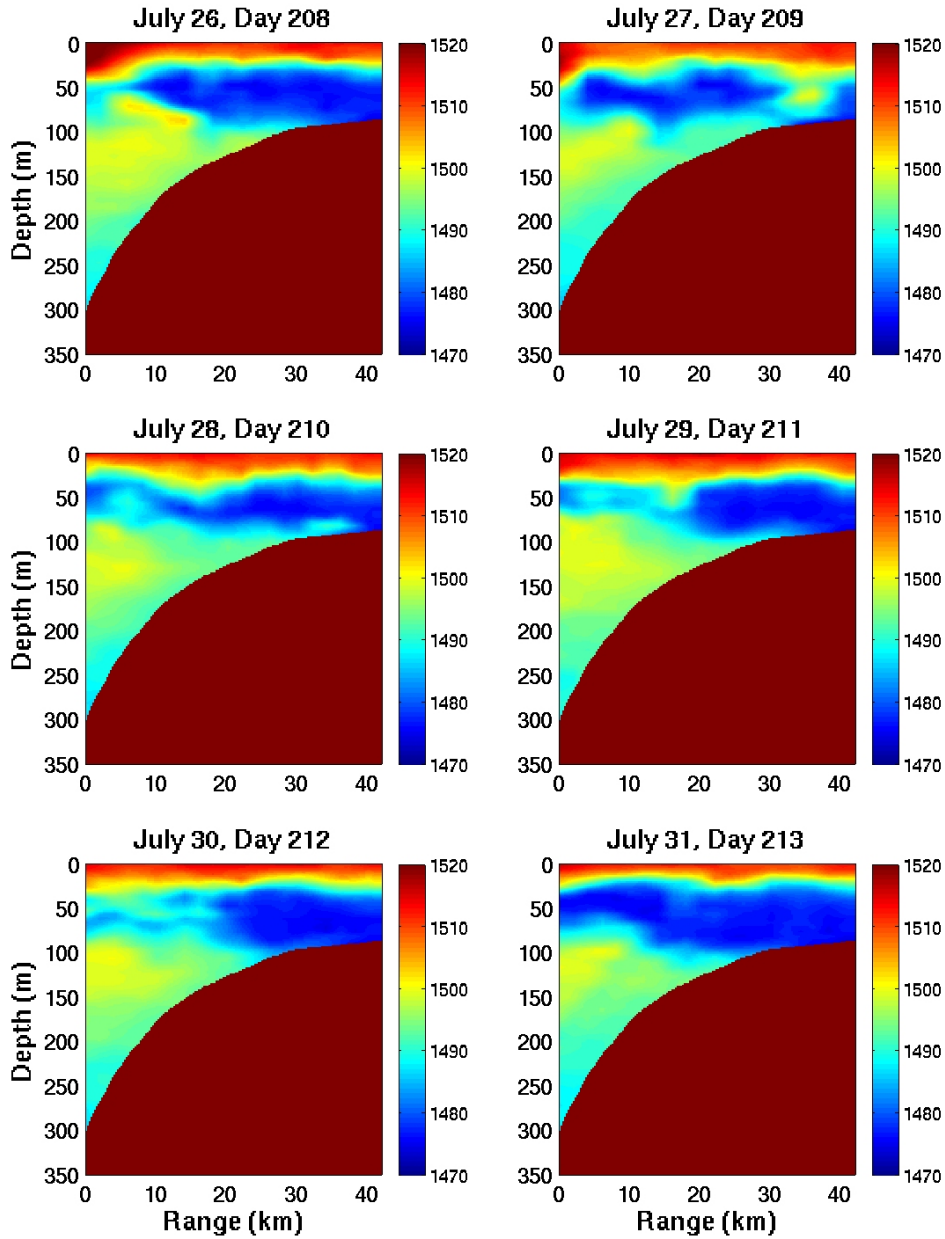


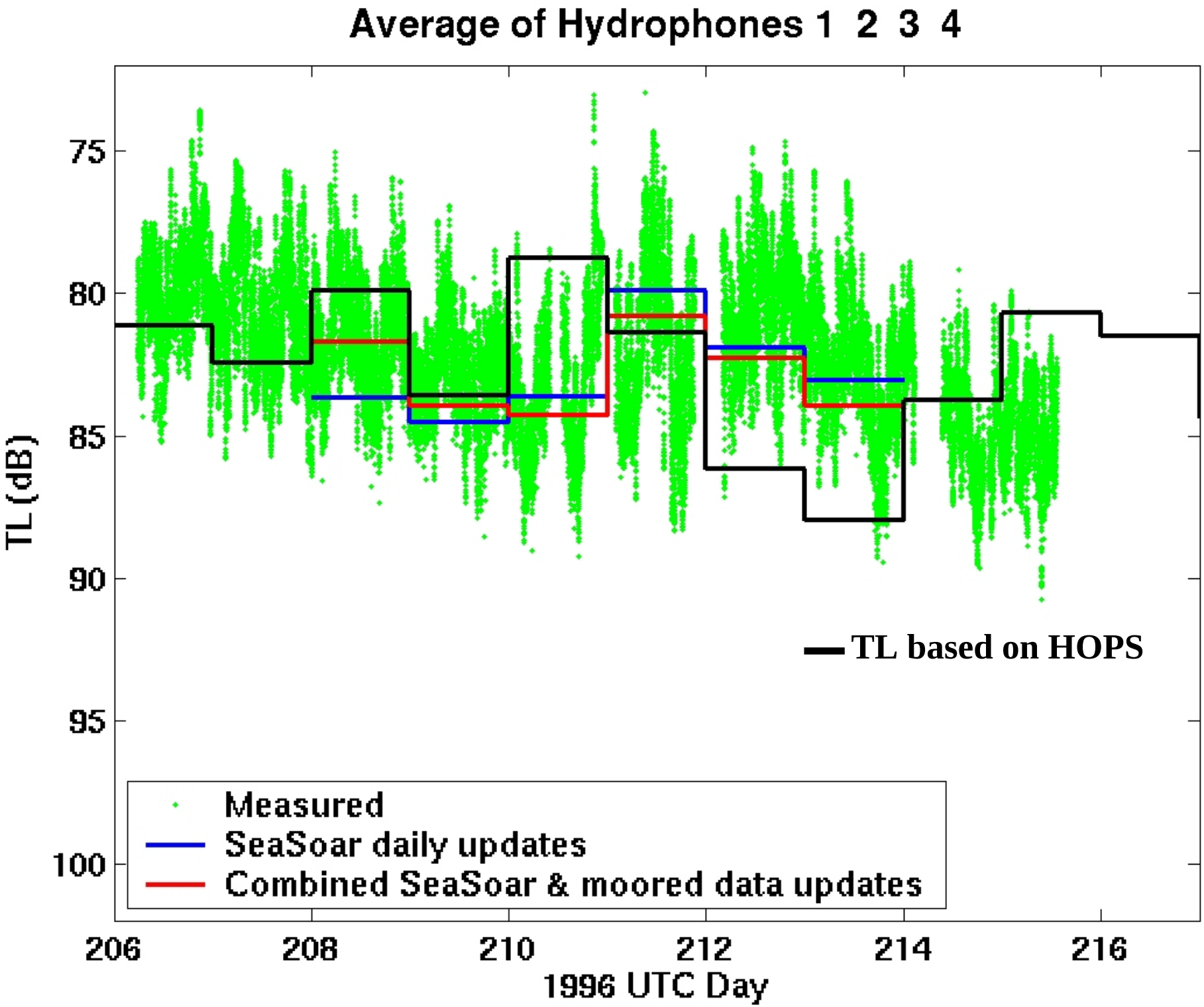
Acoustic Propagation Parameter: HOPS sound-sections at noon time

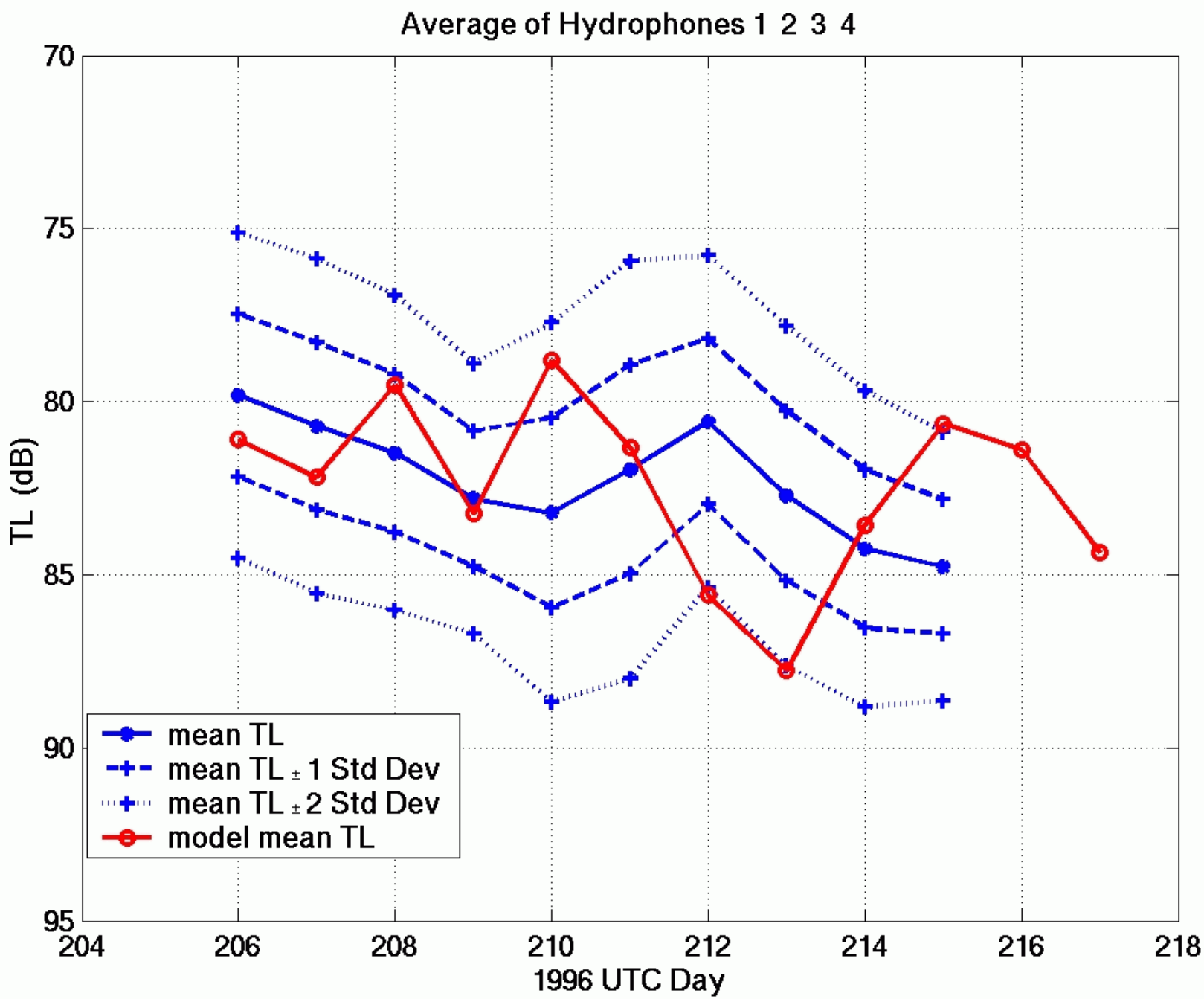
HOPS sections: 3 km grid (6-10 km scale)



Seasoar + moored data (4 km cor. scale)




Average of Hydrophones 1 2 3 4
TL (dB)
75
80
85
90
95
100
206
208
210
212
214
216
1996 UTC Day
TL based on HOPS
Measured
SeaSoar daily updates
Combined SeaSoar & moored data updates

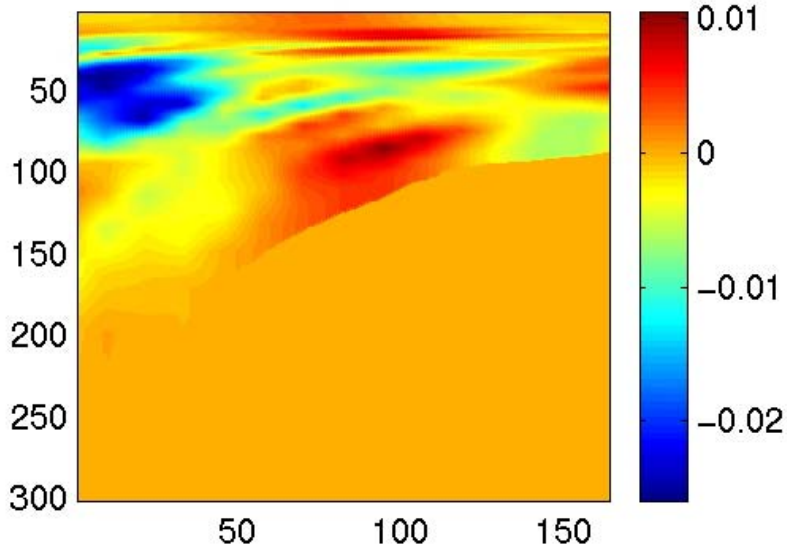

Average of Hydrophones 1 2 3 4
70
75
80
85
90
95
TL (dB)
204
206
208
210
212
214
216
218
1996 UTC Day
mean TL
mean TL ± 1 Std Dev
mean TL ± 2 Std Dev
model mean TL

Coupled Physical-Acoustical Data Assimilation of real TL data: Eigenmodes of coupled normalized error covariance on Jul 26

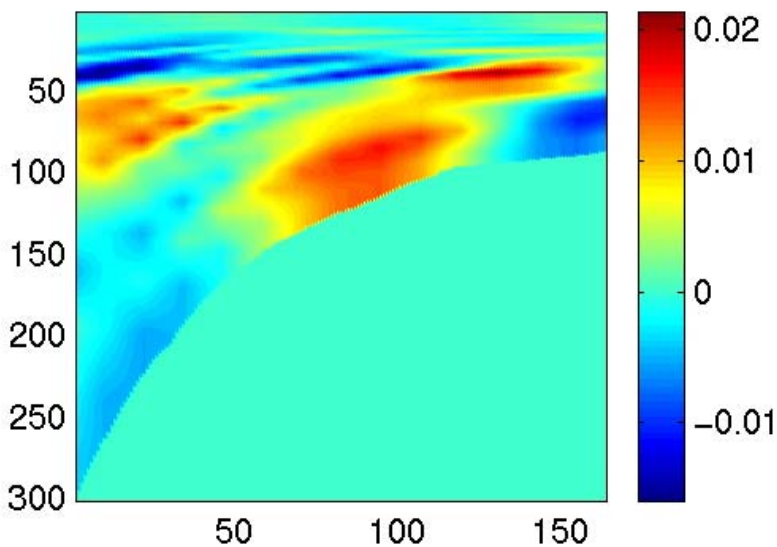
Mode 1

Mode 2

Sound-speed Component

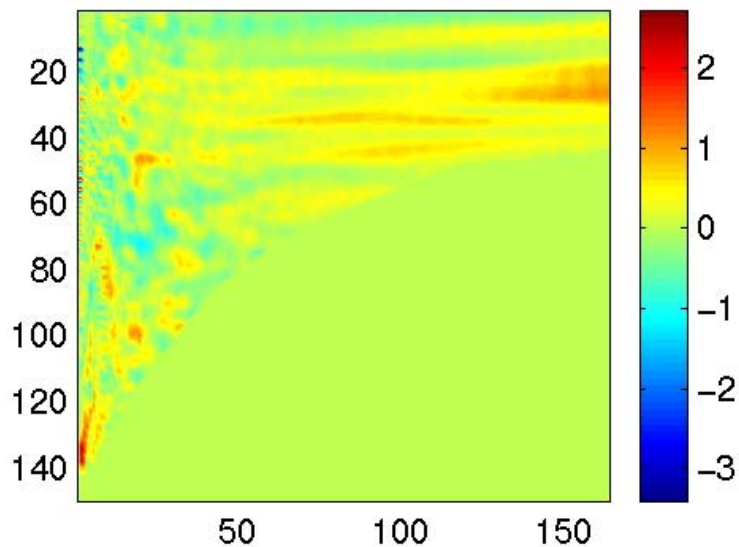


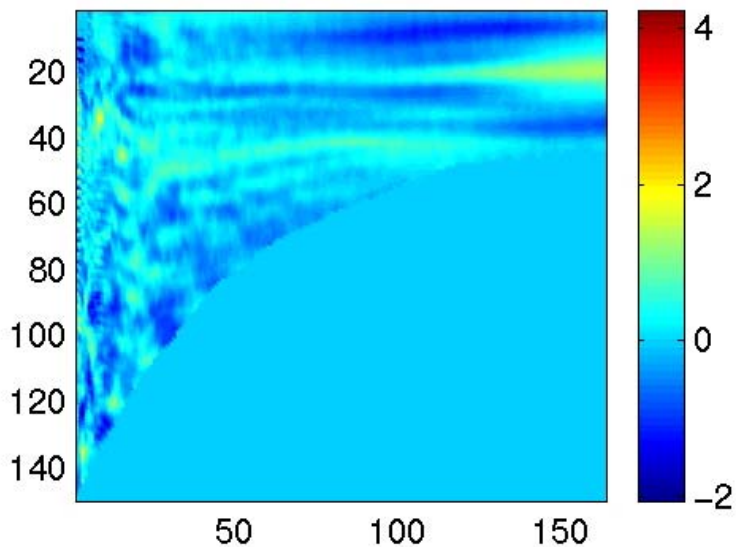
Shift in frontal shape (meander) and its acoustic TL above source and cold channel



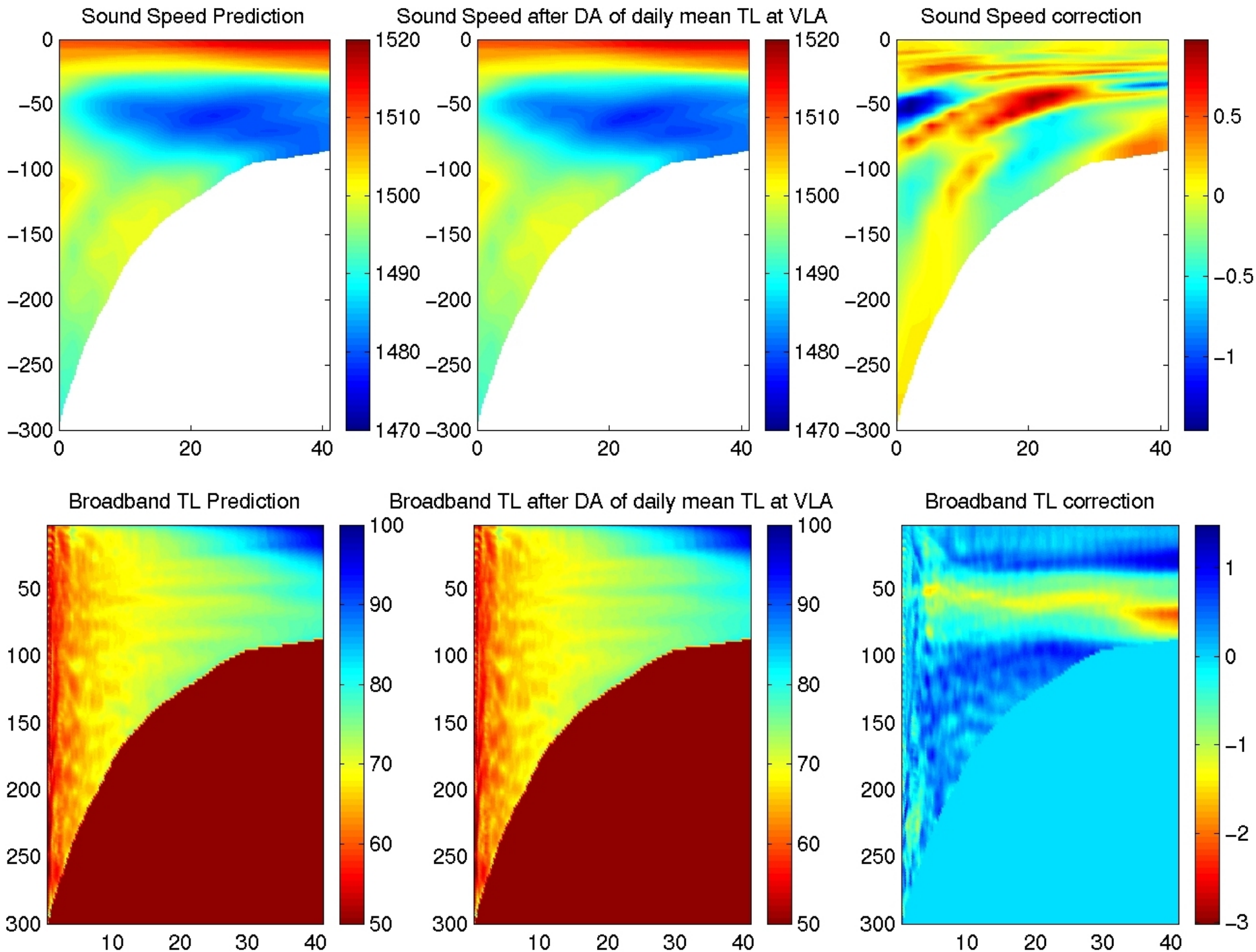
Opposition to mode 1 + surface thermocline tilt and depth with bottom couling at the source

Broadband TL Component

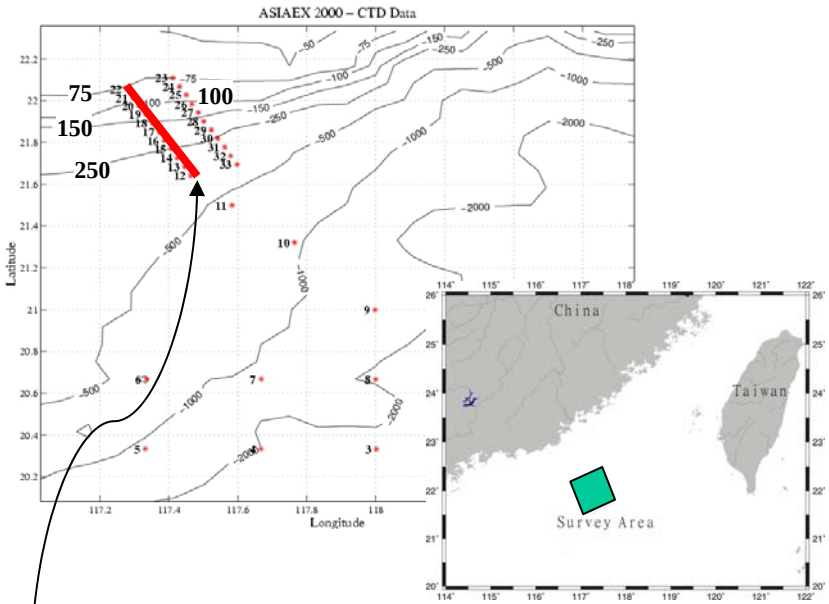


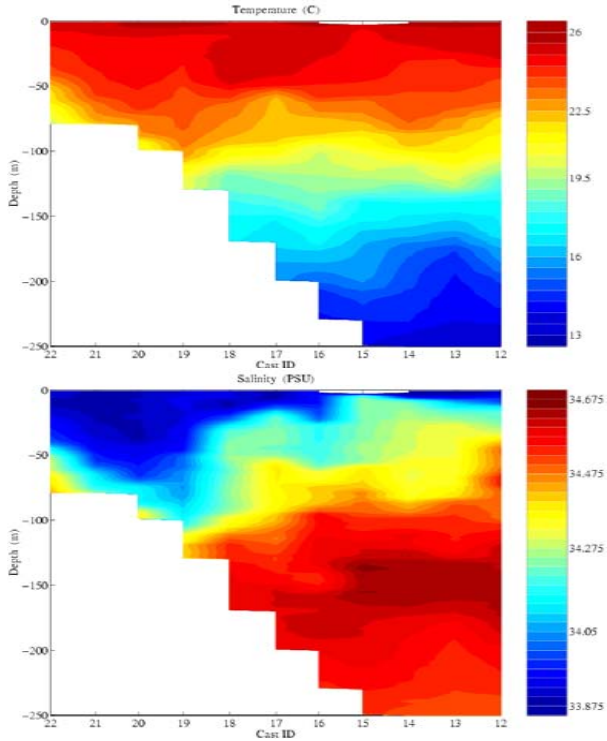


Coupled Physical-Acoustical Data Assimilation of real TL data



ASIAEX – April 2000





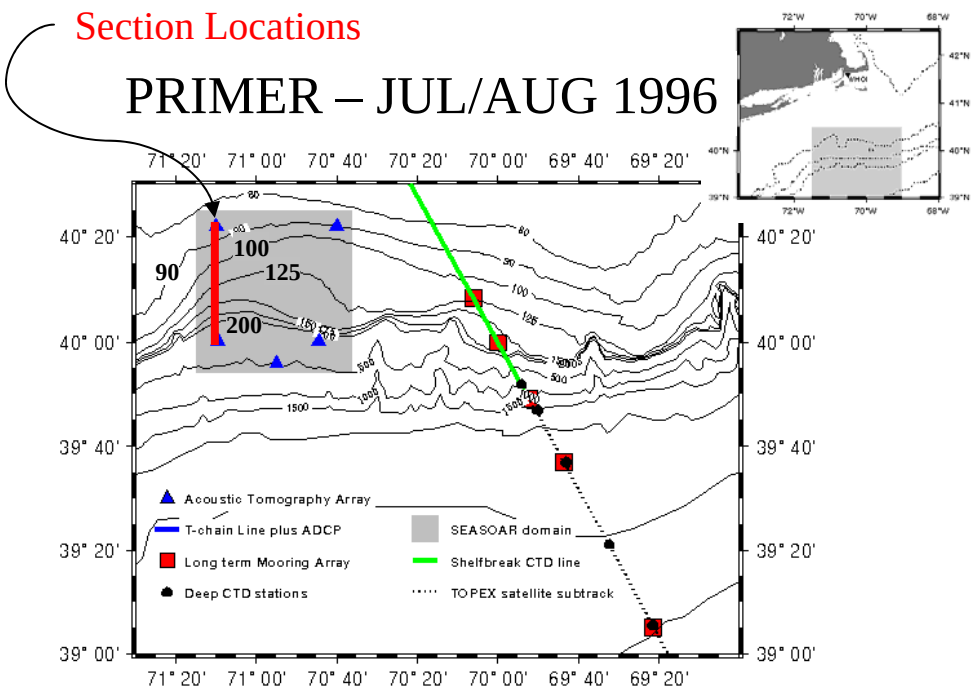
Temperature

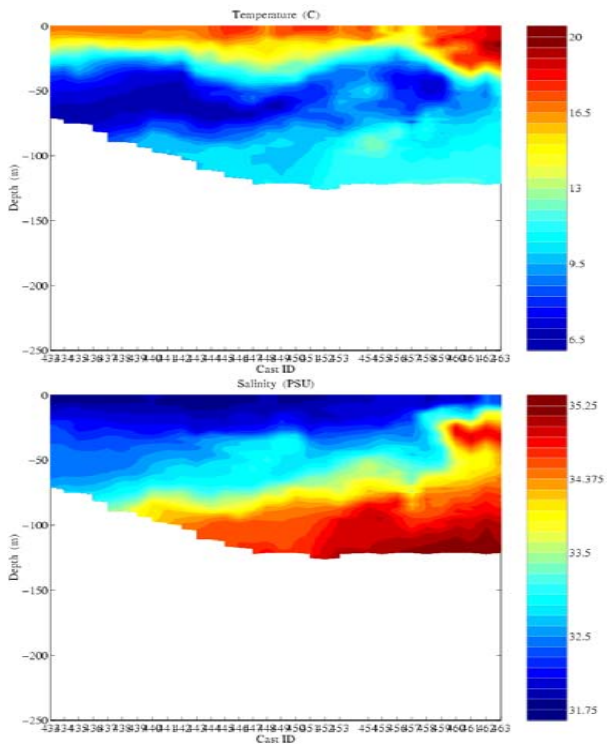
NW-SE Section near
117.4E (~50km)
19 April 2000

Salinity

Section Locations

PRIMER – JUL/AUG 1996





Temperature

N-S Section along
71.15W (~44km)
28 July 1996

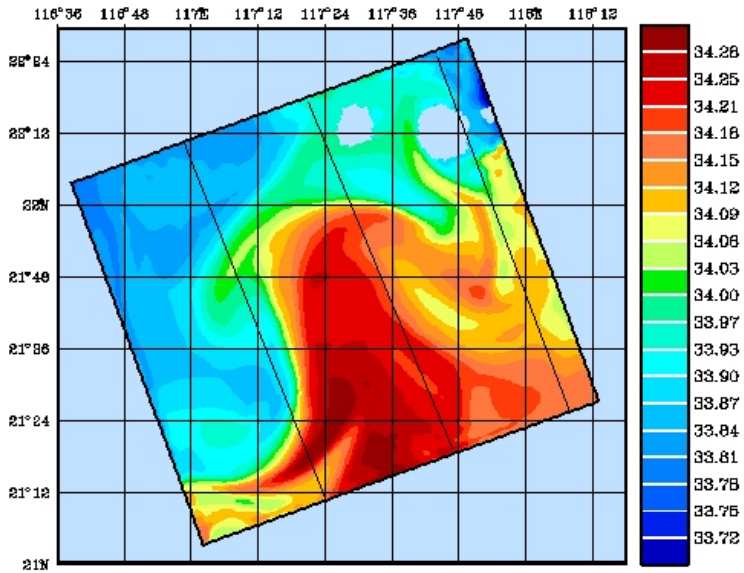
Salinity

Comparison of PRIMER ’96 and ASIAEX ’00 Shelfbreak Fronts

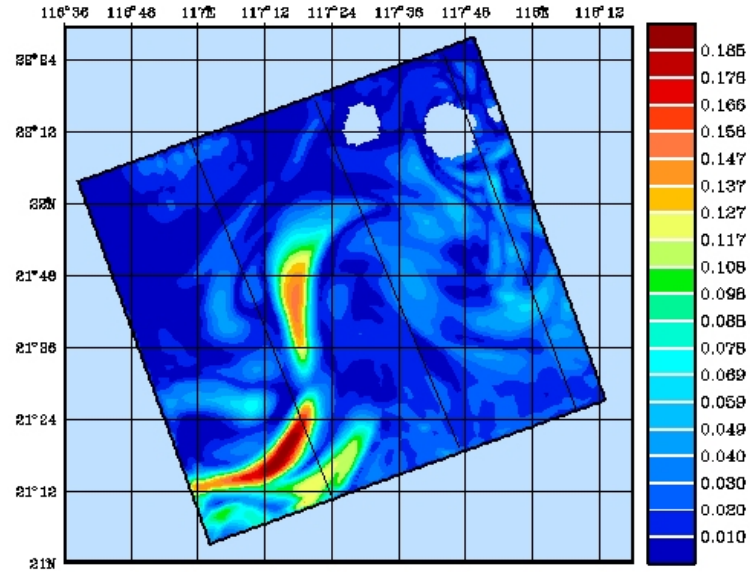
	PRIMER	ASIAEX
Temp. Range of Section	6.5 – 20°	13 – 26°
Salinity Range of Section	31.75 – 35.25 PSU	33.875 – 34.675 PSU
Salinity Difference across Front	~1.625 PSU	~0.2 PSU
Slope	.0020	.0023
Width	5 – 10 km	5 – 20 km
Foot	100m	110m
Notable	Strong surface heating	Front not always present (e.g. 2001)

Ensemble statistics for ASIAEX 2000

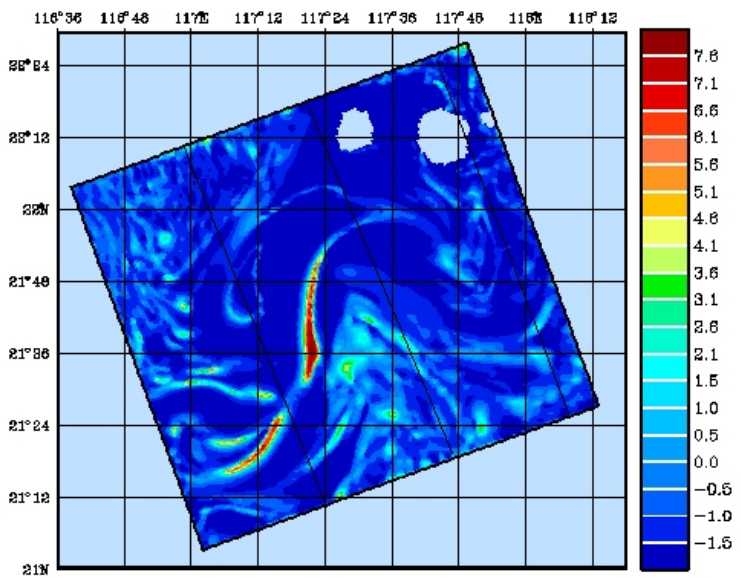
30m Salinity; 15 members



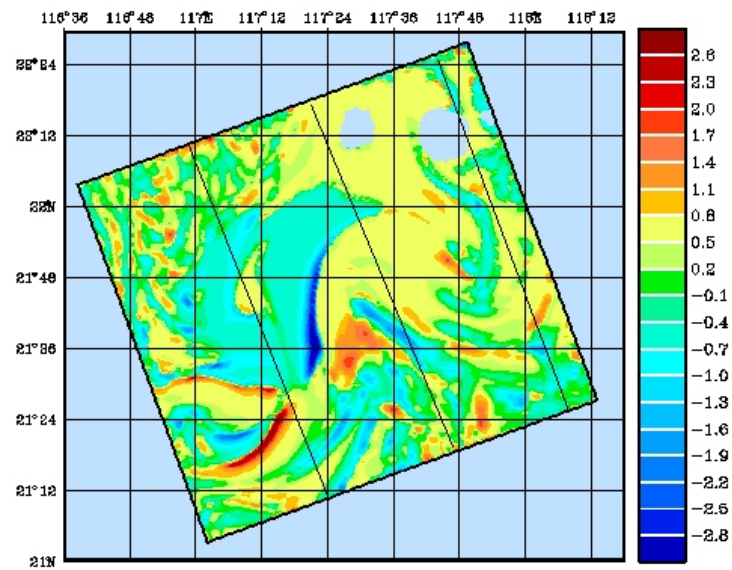
Mean



Standard Deviation



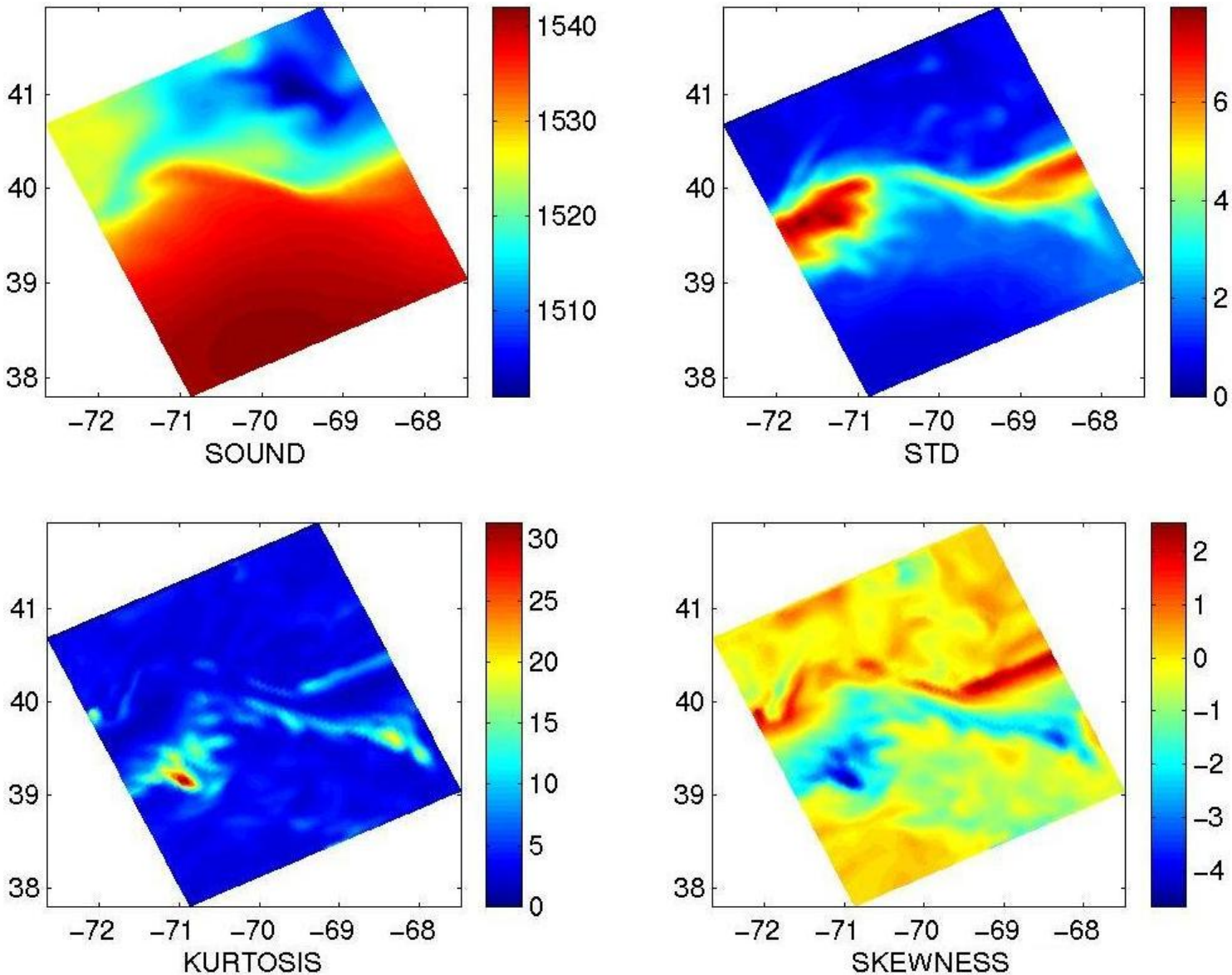
Kurtosis



Skewness

Ensemble statistics for PRIMER 1996

Surface Sound Speed; 80 members

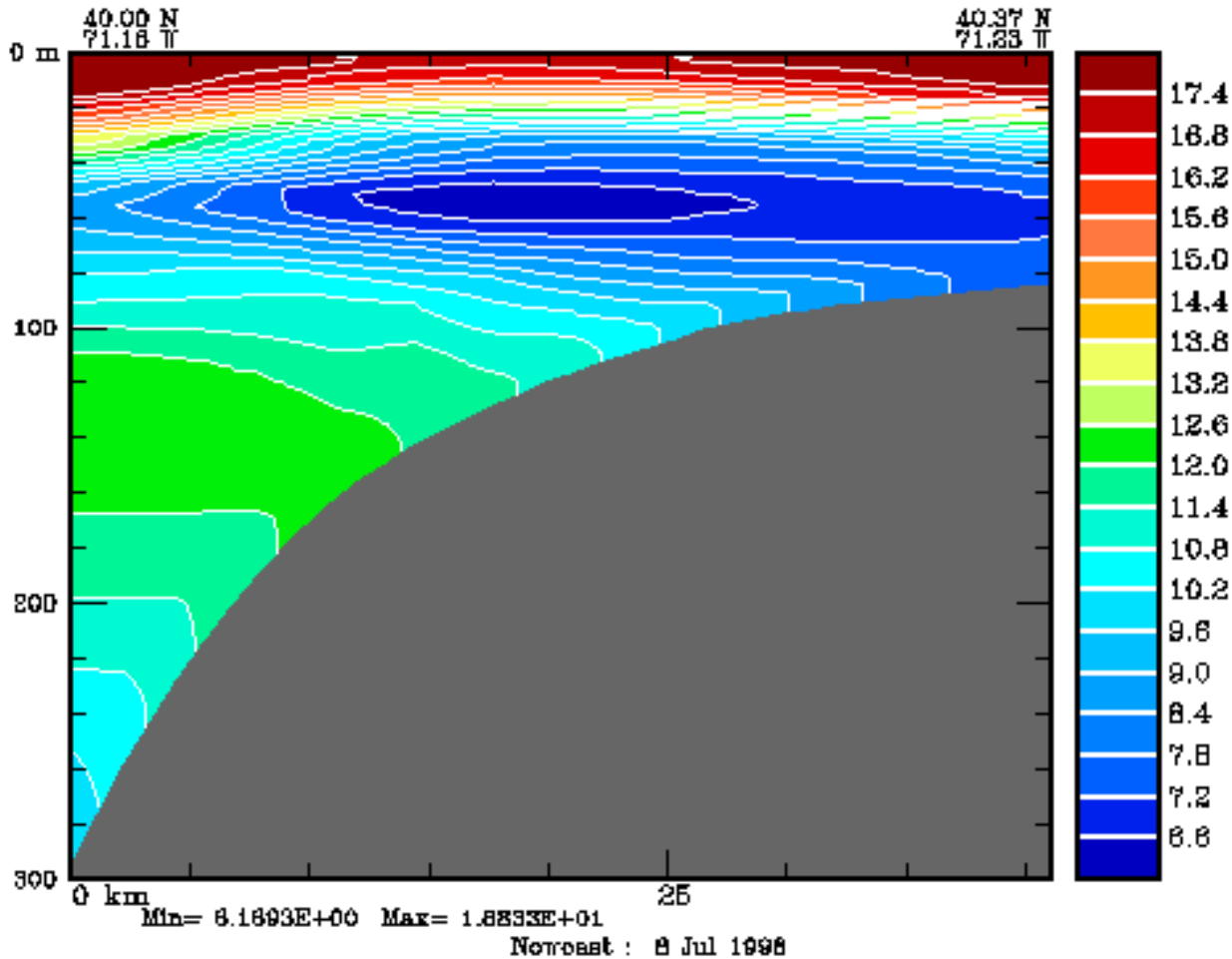


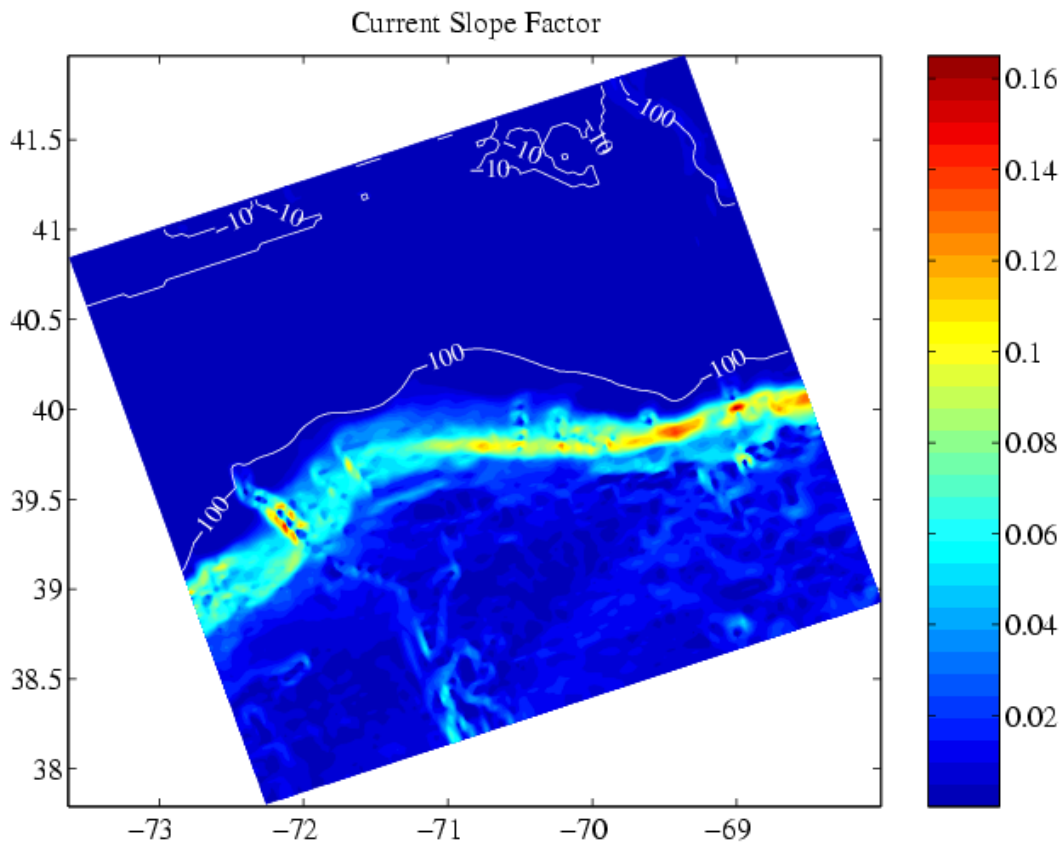
CONCLUSIONS

- Achieved 1-month simulation of ocean physics and its uncertainties at accuracy useful for acoustic propagation predictions
  - Ocean prediction acoustically useful even at times where there is no physical data
  - Requires steep topographies and intensive parameter estimation/fit, but is feasible today
- Shelfbreak PRIMER oceanic processes:
  - Large meander captured (prior to data assimilation). Arises due to a combination of internal ocean instabilities and atmospheric forcing
  - (Sub)-mesoscale eddy field at the front important in summer conditions and similar to open ocean eddies
- Most multiple sources of physical uncertainties accounted and predicted using dominant error approach of ESSE: non-stationary error statistics
- Oceans physics/acoustics data assimilation via ESSE: carried-out with real data as a single multi-scale joint estimation for the first time, using higher-moments to characterize uncertainties
  - Corrects too lossy TL at depth (2 db) and two high in surface mixed layer
  - Leads to corrections in whole acoustic section within cold channel and to shift in sound-speed front above the source (slope water meander/eddy)

EXTRA VUGRAFS

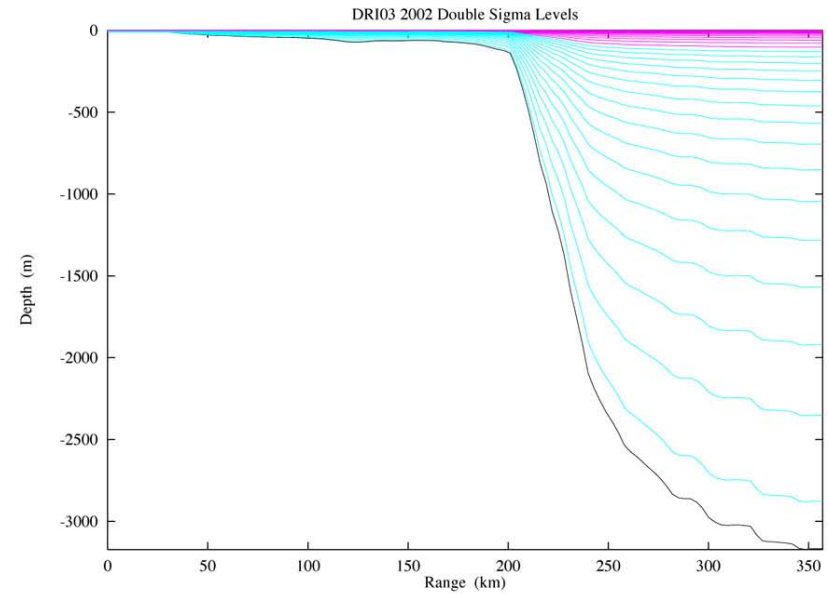
Temperature along Western Acoustic Track
8 July – 7 August 1996

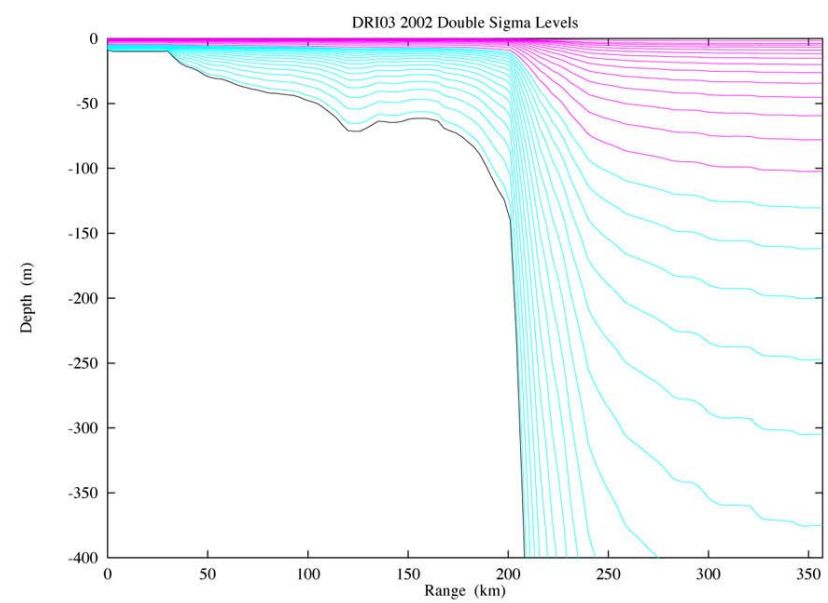




Case 13 (Conditioned): C=4.7, $\alpha = 0.04$

-73.4818 40.8695 **-72.1200 37.8340**





STOCHASTIC FORCINGS MODEL: Sub-grid-scales

I. 0d Random Noise Exponentially Decorrelated in Time

$$d\tilde{w} + \beta\, \tilde{w}\, dt = dw, \tag{76}$$

$$\dot{p}_{\tilde{w}} = -2\beta\, p_{\tilde{w}} + q \ . \tag{77}$$

Setting $\dot{p}_{\tilde{w}}$ to zero at all times yields $p_{\tilde{w}}(0) = \sigma^2 = \frac{q}{2\beta}$. The process $\tilde{w}$ is assumed to be of fixed fluctuation amplitude σ and autocorrelation time $\frac{1}{\beta}$. The constant variance of the white noise w is thus set to $q = 2\beta\sigma^2$.

II. 3d Random Noise, Exponentially Decorrelated in Time and 2-Grid Point Decorrelated in Space

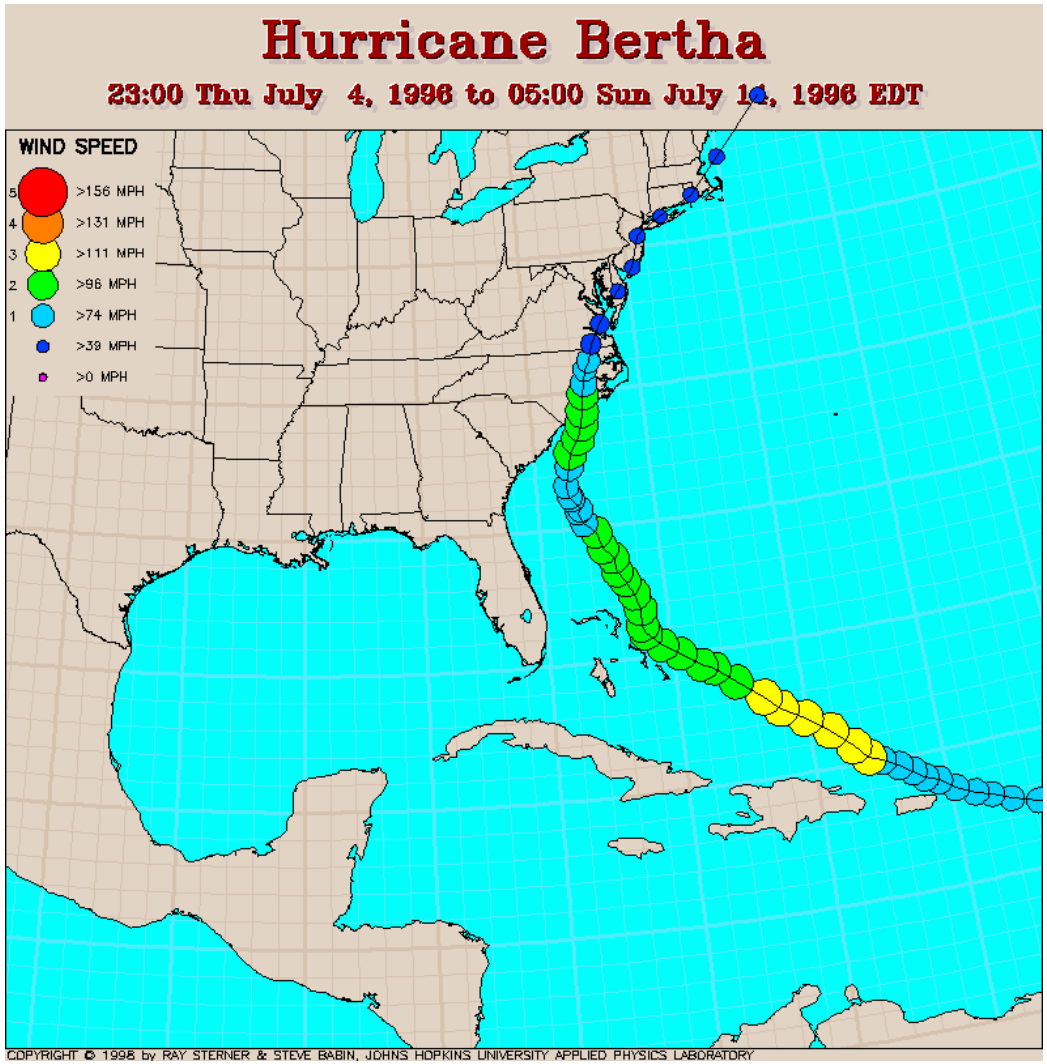
$$\mathbf{d}\boldsymbol{\psi}^t = \mathbf{f}^{PE}\big(\boldsymbol{\psi}^t, t\big)\ dt + \mathbf{B}^{fc}(t)\ \mathbf{d}\tilde{\mathbf{w}}^c\ . \tag{86a}$$

$$\mathbf{d}\tilde{\mathbf{w}}^c = -\boldsymbol{\beta}^c \tilde{\mathbf{w}}^c\, dt + \mathbf{d}\mathbf{w}^c\ , \tag{86b}$$

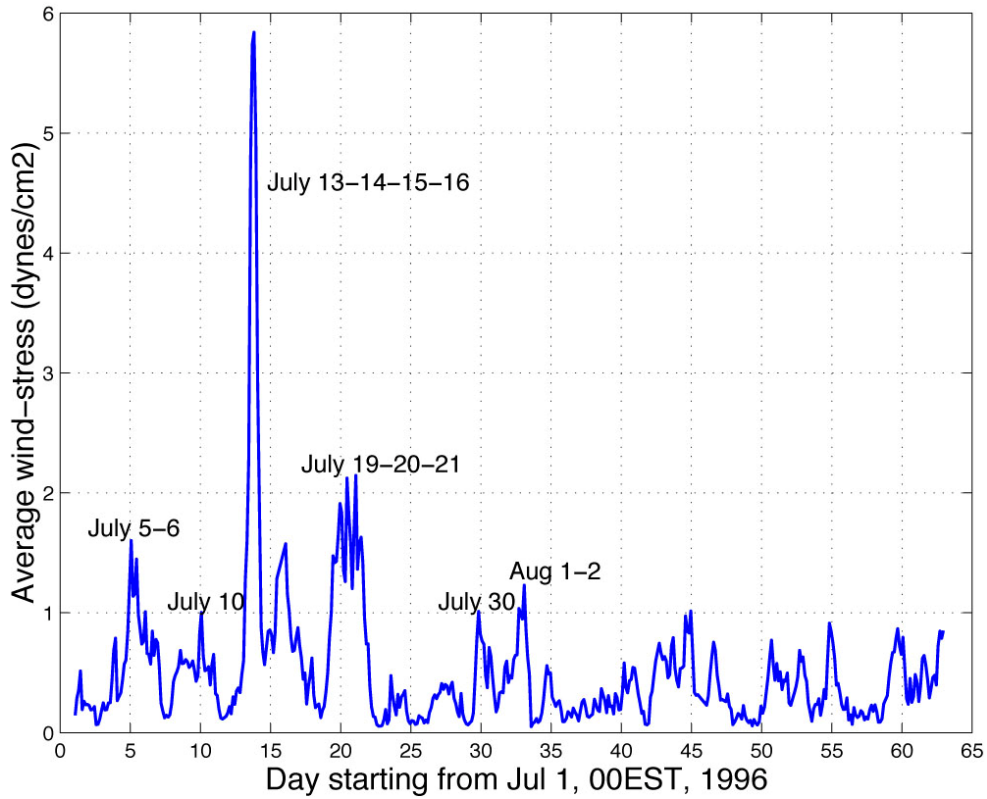
where symbols denote the:

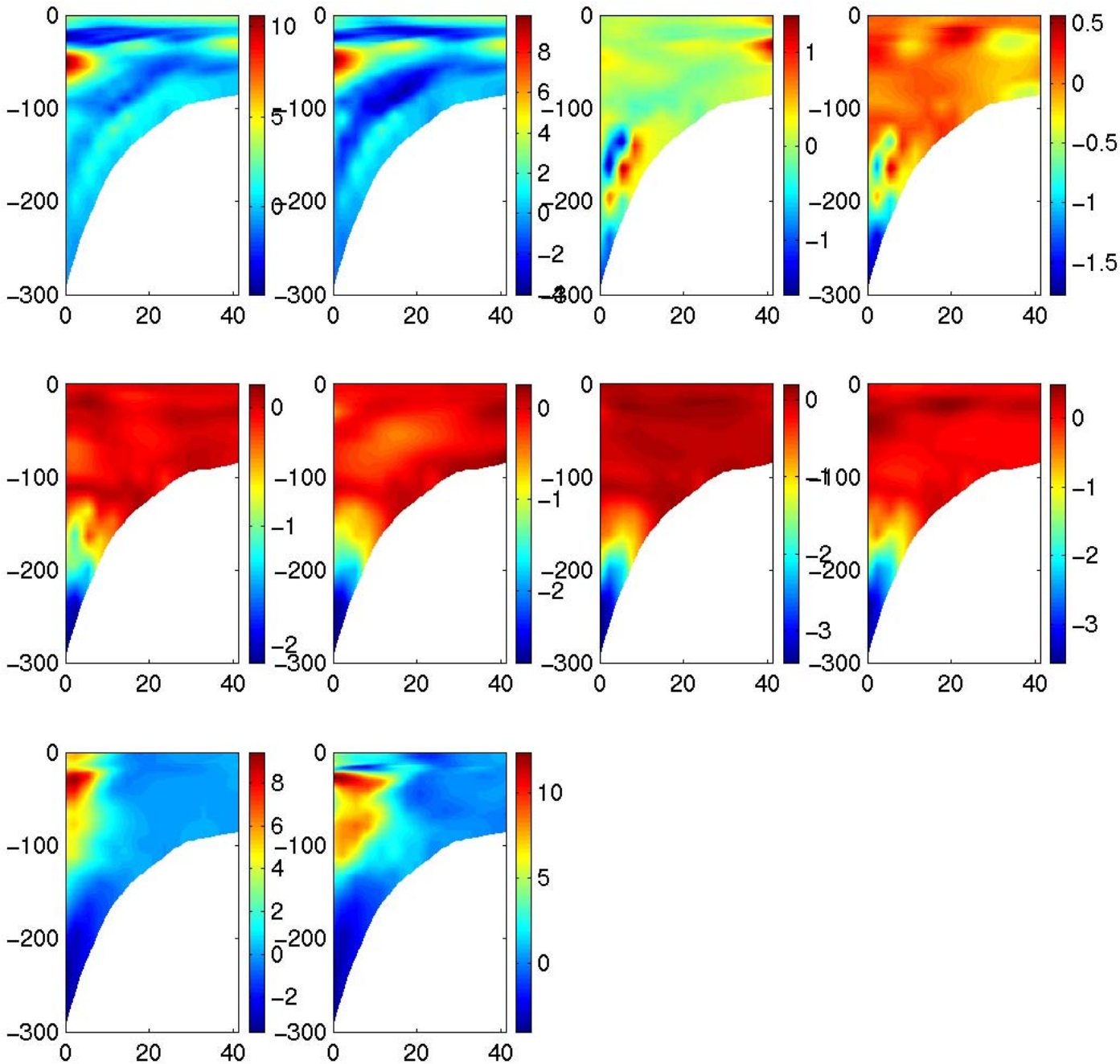
- **discrete-space PE state vector:** $\boldsymbol{\psi} = (\hat{\mathbf{u}}, \hat{\mathbf{v}}, \mathbf{T}, \mathbf{S}, \mathbf{p})^T \in \mathbb{R}^n$
- **coarse 3d white noise:** $\mathbf{w}_k^c$
- **Coarse 3d Gauss-Markov process:** $\tilde{\mathbf{w}}_k^c$**,**

  i.e. $\mathbf{d}\mathbf{w}^c = (\mathbf{d}\mathbf{w}_{\hat{u}}^c, \mathbf{d}\mathbf{w}_{\hat{v}}^c, \mathbf{d}\mathbf{w}_T^c, \mathbf{d}\mathbf{w}_S^c, \mathbf{d}\mathbf{w}_\psi^c)^T$
- **PE dynamical model operator:** $\mathbf{f}^{PE}\big(\cdot, t\big)$
- **linear extrapolation matrix, from coarse to fine state:** $\mathbf{B}^{fc}(t)$

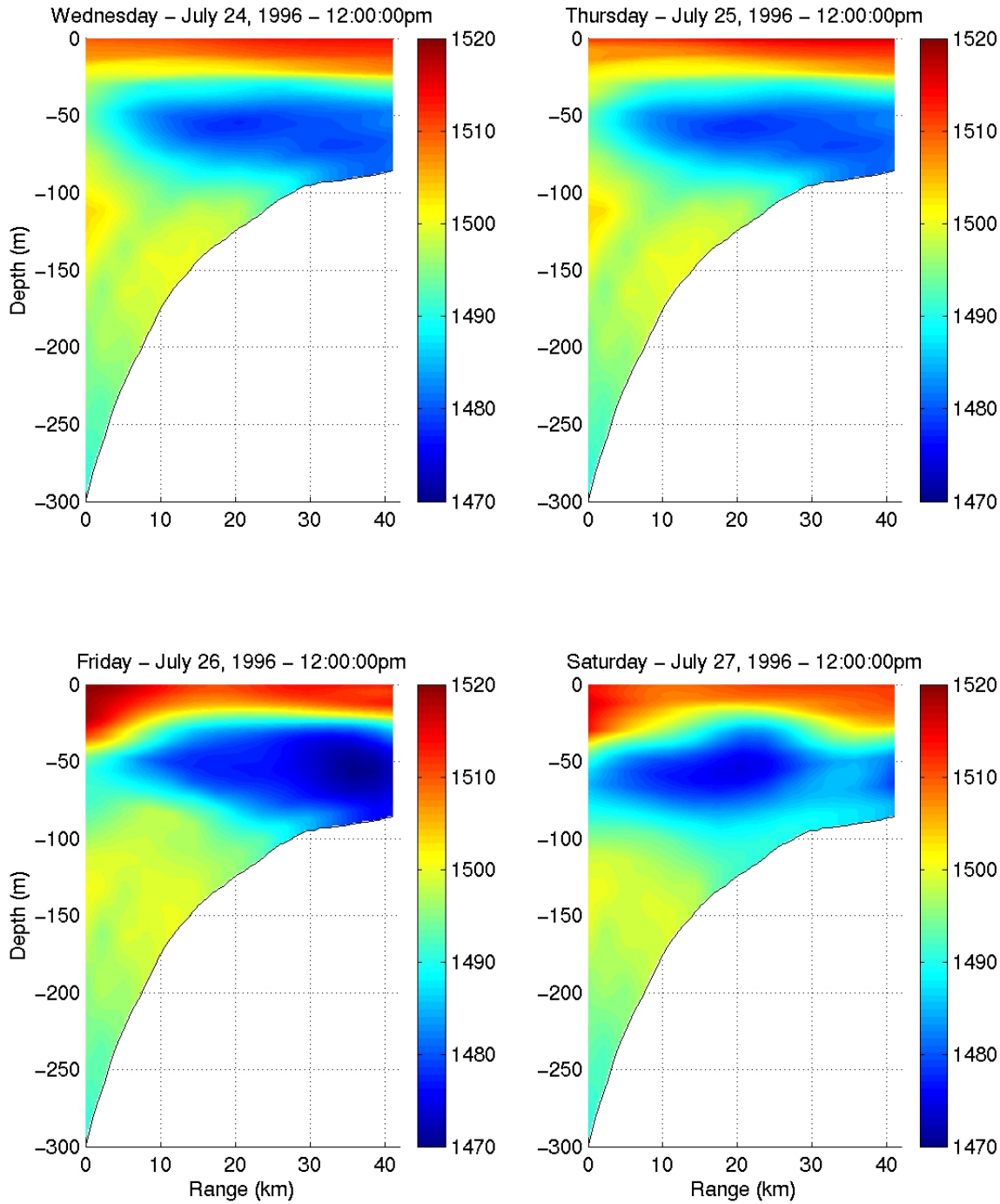


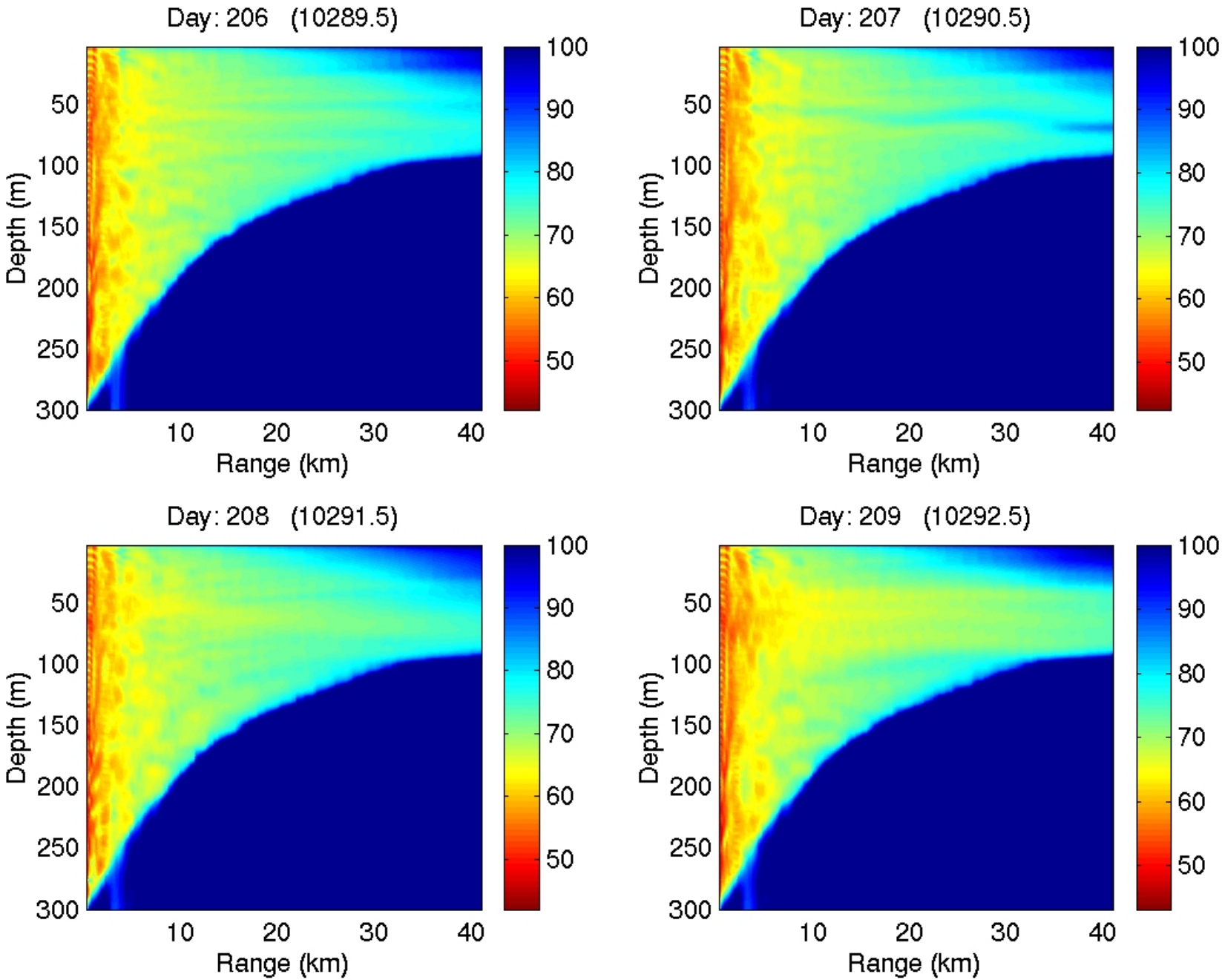
Averaged wind-stress time-series

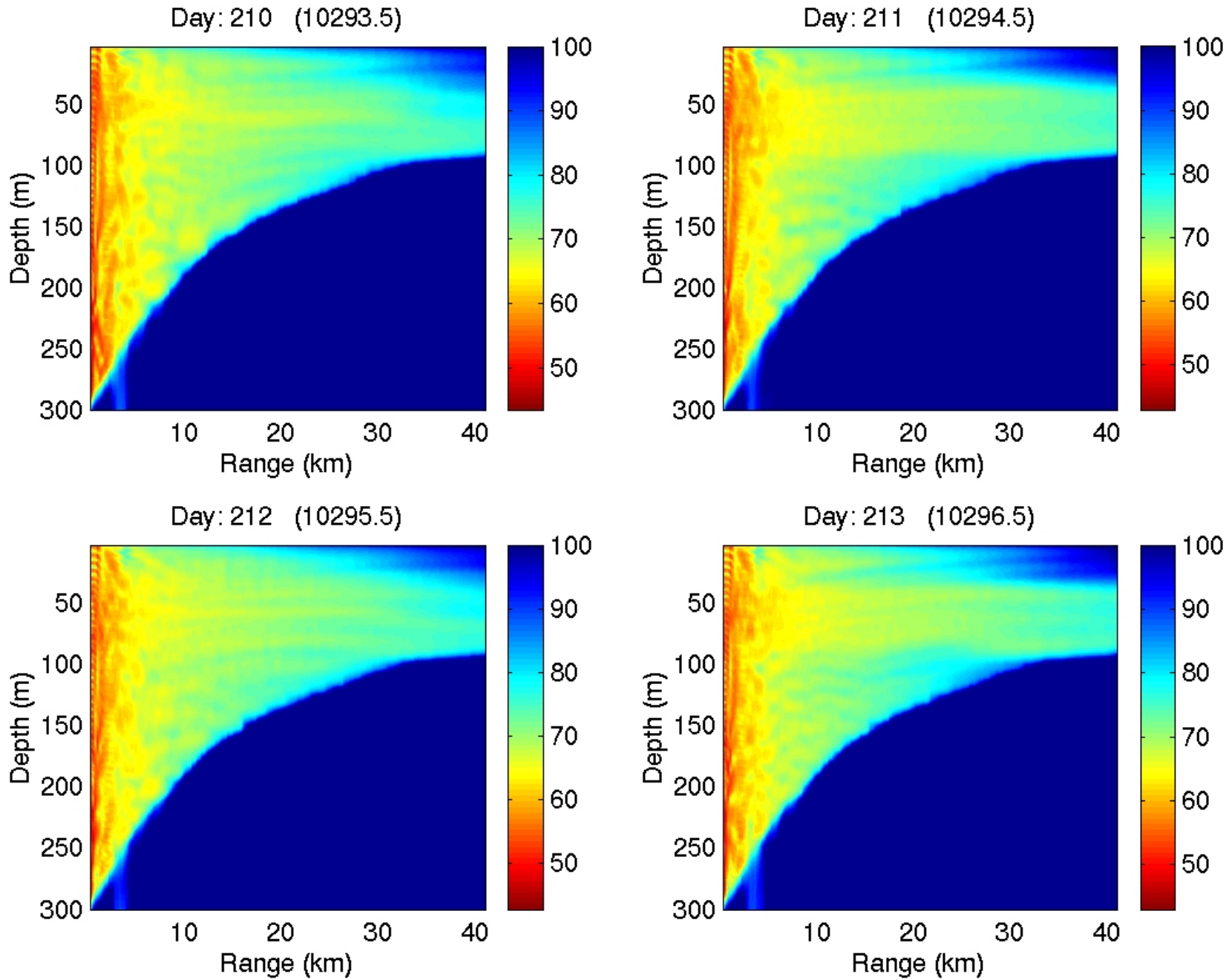


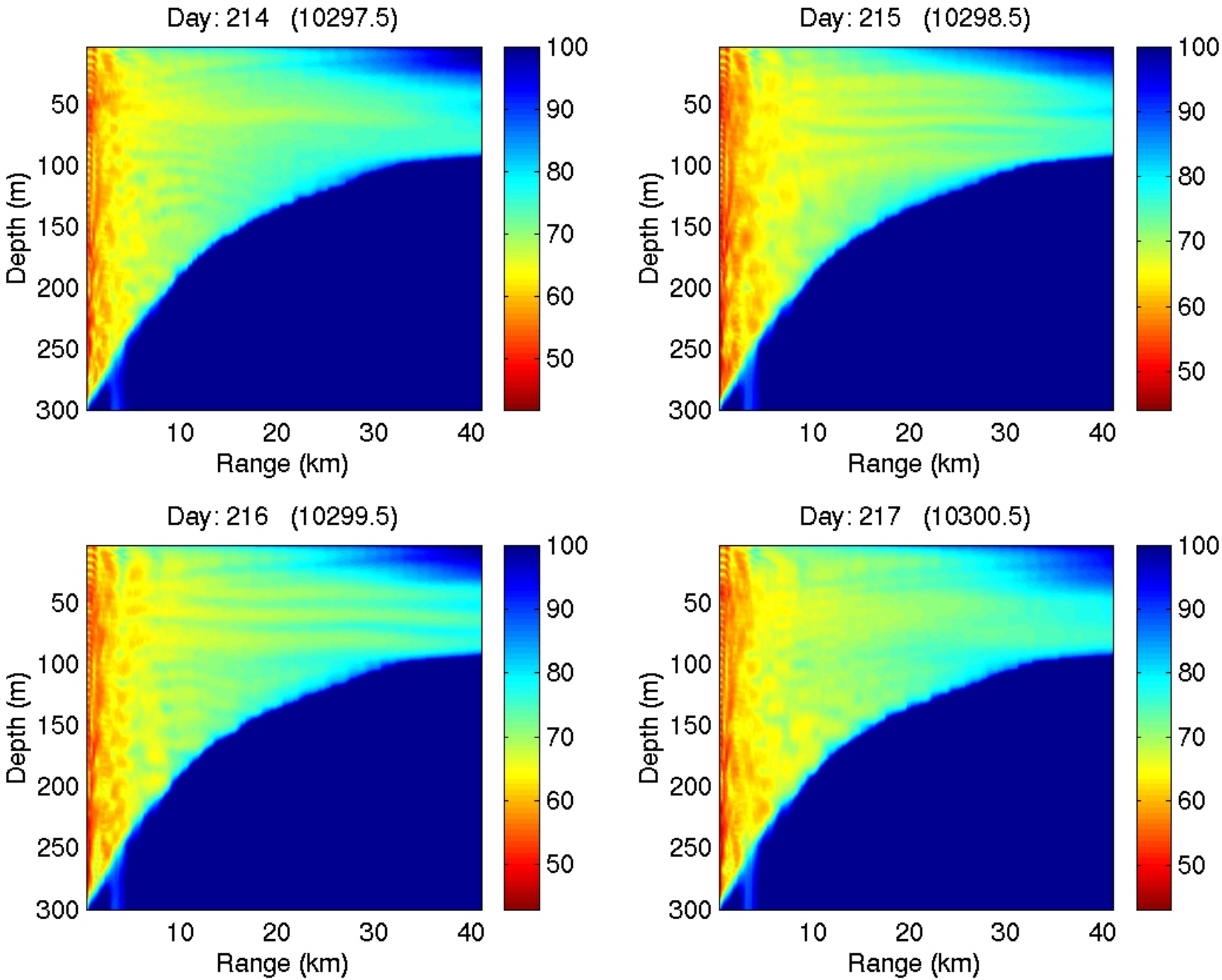

0
−100
−200
−300
0
20
40
10
5
0
8
6
4
2
0
−2
−4
1
0
−1
0.5
0
−0.5
−1
−1.5
0
−1
−2
−3
8
6
4
2
0
−2
10
5
0

Daily realizations of section 1 (SRC: −71.1628,40.0022); VLA: −71.226,40.3684)




Day: 206 (10289.5)
Day: 207 (10290.5)
Day: 208 (10291.5)
Day: 209 (10292.5)
Depth (m)
Range (km)
50
100
150
200
250
300
10
20
30
40
100
90
80
70
60
50


Day: 210 (10293.5)
Day: 211 (10294.5)
Day: 212 (10295.5)
Day: 213 (10296.5)
Depth (m)
Range (km)
50
100
150
200
250
300
10
20
30
40
100
90
80
70
60
50


Day: 214 (10297.5)
Day: 215 (10298.5)
Day: 216 (10299.5)
Day: 217 (10300.5)
Depth (m)
Range (km)
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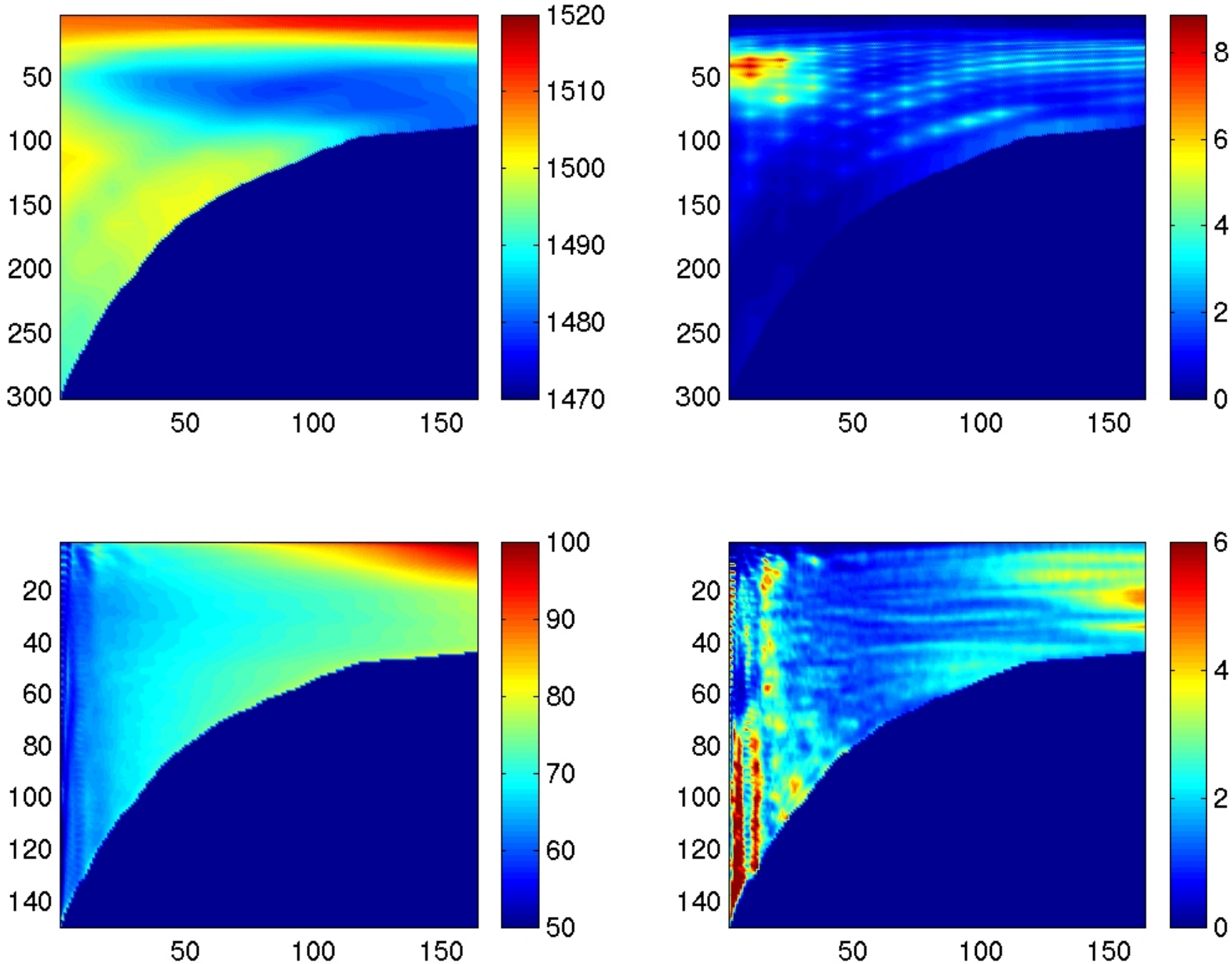
100
150
200
250
300
10
20
30
40
100
90
80
70
60
50


50
100
150
200
250
300
50
100
150
1520
1510
1500
1490
1480
1470
50
100
150
200
250
300
50
100
150
8
6
4
2
0
20
40
60
80
100
120
140
50
100
150
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120
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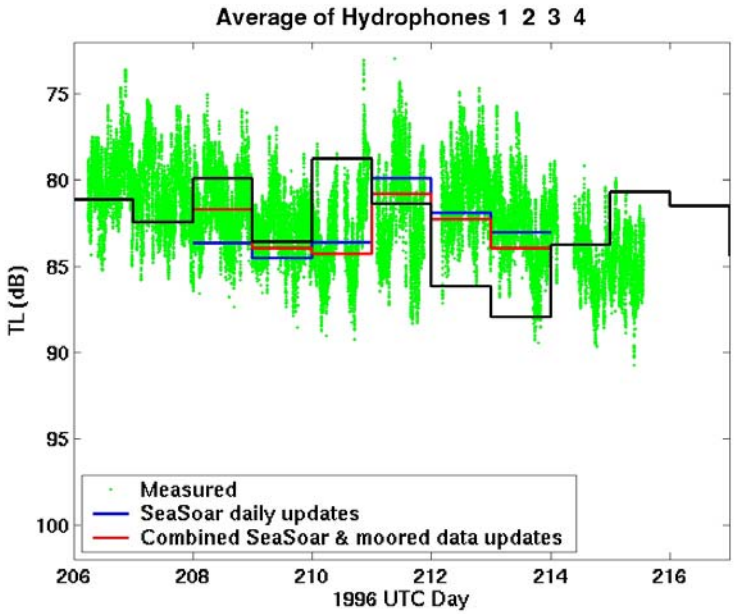
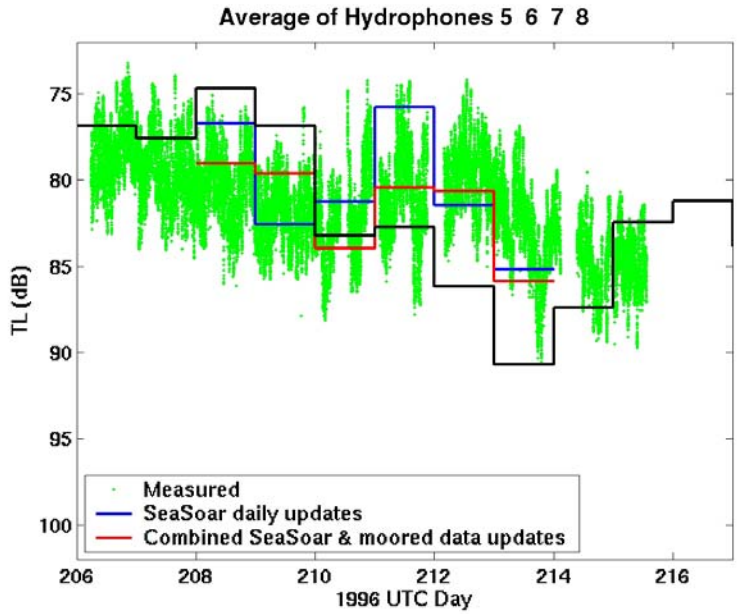
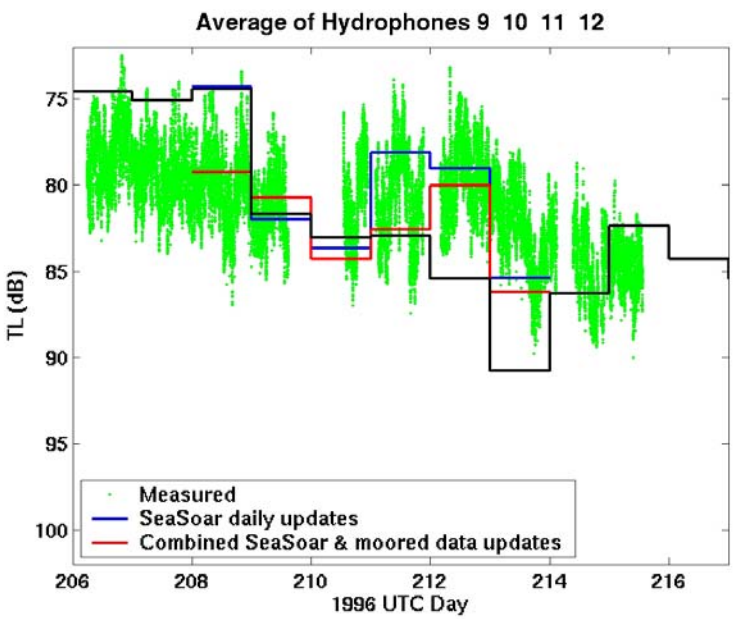
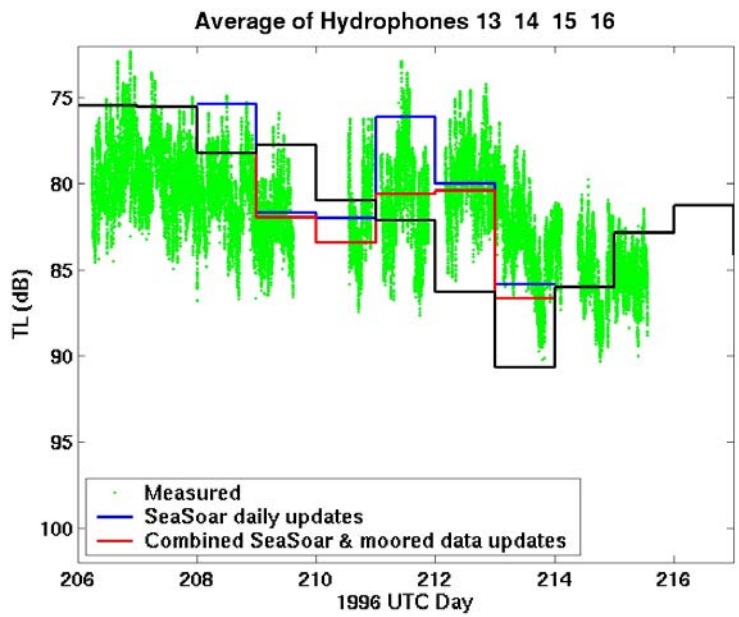
100
150
6
4
2
0


Average of Hydrophones 1 2 3 4
TL (dB)
1996 UTC Day
Measured
SeaSoar daily updates
Combined SeaSoar & moored data updates


Average of Hydrophones 5 6 7 8
TL (dB)
1996 UTC Day
Measured
SeaSoar daily updates
Combined SeaSoar & moored data updates


Average of Hydrophones 9 10 11 12
TL (dB)
1996 UTC Day
Measured
SeaSoar daily updates
Combined SeaSoar & moored data updates


Average of Hydrophones 13 14 15 16
TL (dB)
1996 UTC Day
Measured
SeaSoar daily updates
Combined SeaSoar & moored data updates