Extended-Range Prediction with Low-Dimensional, Stochastic-Dynamic Models: A Data-driven Approach

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LONG-TERM GOALS

The long-term goal of this project is to quantify the extent to which reduced-order models can be used for the description, understanding and prediction of atmospheric, oceanic and sea ice variability on time scales of 1–12 months and beyond.

OBJECTIVES

Demonstrate the ability of linear and nonlinear, stochastic-dynamic models to capture the dominant and most predictable portion of the climate system’s variability. Improve the understanding and prediction of the low-frequency modes (LFMs) of variability such as the Madden-Julian Oscillation (MJO), El Niño–Southern Oscillation (ENSO), North Atlantic Oscillation (NAO) and Pacific–North American (PNA) pattern. Validate LDMs based on data sets from observations, reanalyses and high-end simulations.
APPROACH

Methodological developments. Develop and improve further the empirical model reduction (EMR) methodology for nonlinear stochastic inverse modeling (Kondrashov et al., 2005, 2006, 2011; Kravtsov et al., 2005, 2009), as well as other low-dimensional models (LDMs), in combination with the recently developed, past-noise forecasting (PNF) methodology for prediction (Chekroun et al., 2011).

Michael Ghil, Mickaël D. Chekroun, Dmitri Kondrashov.

ENSO and coupled variability on seasonal time-scales. Improve understanding and prediction of ENSO, tropical Atlantic variability (TAV), and the Indo-Pacific coupled mode (IPT).

Mark Cane, David Chapman, Chen Chen, Naomi Henderson, Alexey Kaplan, Dong Eun Lee.

MJO. Our goal in this work is to understand what kind of dynamical mode the MJO is, and what its essential ingredients are. This information will then inform prediction. Our conceptual model here is low-order models for ENSO, such as the Cane-Zebiak model, that have been so important for prediction — in their direct use as forecast models, as well as in the understanding they have generated.

Adam Sobel, Daehyun Kim and Shuguang Wang.

Extratropical variability and predictability. Determine the extent to which extratropical monthly and seasonal low-frequency variability (LFV, i.e. PNA, NAO, as well as other regional blocking patterns) can be skillfully predicted for 1–12 months in advance in an LDM that includes ENSO, MJO and stratospheric linkages. Characterize statistically extratropical storms and extremes, and link these to LFV modes.

Mingfang Ting, Yochanan Kushnir, Andrew W. Robertson, Lei Wang.

Downscaling Weather and Seasonal Climate. Use LDMs to relate near-surface temperature and precipitation with predictable climate forcing such as SSTs. Explore the development of statistical tropical-cyclone (TC) forecasts based on ENSO and MJO forecasts by LDMs. Target tropical monsoon climates, emphasizing sub-seasonal characteristics of weather, such as rainfall and drought extremes.

Andrew W. Robertson, Suzana J. Camargo, Yochanan Kushnir, Michael K. Tippett, John Allen.

Sea Ice. Inrasonal and annual prediction of Arctic sea ice, improve Antarctic sea ice forecasts and assess the impact of sea ice on mid-latitude predictability.

Xiaojun Yuan, Dake Chen, Lei Wang.

WORK COMPLETED

Kick-off meeting on October 6, 2012 in Palisades, NY, for UCLA and CU researchers and ONR/DoD program managers Scott Harper, Reza Malek-Madani and Fariba Fahroo.

New postdoctoral research scientists hired: John Allen, David Chapman, Chia-Ying Lee and Lei Wang (CU) and Honghu Liu (UCLA).


Data-driven, multilayered low-order stochastic models Kondrashov et al. (2013a) introduced a general class of multilayered stochastic models (MSMs) that fall within the Mori-Zwanzig formalism of statistical physics. These models describe the role played in EMR by the non-Markovian terms that represent the cross-interactions between the resolved and unresolved variables. In EMR, such interactions appear via random difference equations forced by the resolved variables, while feeding back into the resolved dynamics via convolution integrals that involve the history of their fluctuations.
Rough parameter dependence in climate models: The role of Ruelle-Pollicott resonances  Based on the spectral theory of chaotic and dissipative dynamical systems, Chekroun et al. (2013c) have shown that the recurrences observed in planetary flows can play a key role in the parameter dependence of long-term flow statistics. We interpret this dependence in terms of Ruelle-Pollicott (RP) resonances and have developed a new approach based on using Markov representations to estimate these resonances. The relation between the eigenvalues of the resulting Markov operators and the RP resonances shows that a small gap in the dominant fraction of the latter corresponds to regimes where peaks in the power spectrum are the most energetic and correlations decay slowly.

Parameterizing manifolds for stochastic partial differential equations  Chekroun et al. (2013a,b) have developed a general approach for the parameterization of “small” scales in terms of the “large” ones in stochastic partial differential equations (SPDEs) by using parametrizing manifolds (PMs). PMs are stochastic manifolds that improve, in root-mean-square, the partial knowledge of the full SPDE solution vs. its projection onto the resolved modes. PMs are not subject to the classical spectral gap condition: they can be determined under weaker, non-resonance conditions on the eigenvalues associated with the resolved and unresolved modes. Non-Markovian stochastic reduced systems based on such a PM approach appear to perform outstandingly in the modeling of extreme events.

ENSO and coupled variability on seasonal time-scales. A Vector Autoregressive (VAR) model has been developed to predict tropical climate using 12 months of SST data prior to forecast initialization. The model uses SST data for the 12 months before the initialization time, and it shows particular promise for the Atlantic Hurricane Main Development Region (MDR); see Fig. 1.

Development of a low-order dynamical MJO model. We have added two new elements to the nonlinear version of the model: mixed layer ocean coupling, and weak relaxation on the moisture field. These elements represent persistent import of dry subtropical air by the Hadley circulation and the statistically stationary eddies (i.e., those not closely coupled to the MJO itself), and they allow perturbations to the model physics to change the MJO without destroying the mean state; see Fig. 2.

Analysis of MJO observations. We have analyzed MJO observations in a way designed to constrain the low-order model, in particular its moist static energy (MSE) budget. The MSE budget was analyzed using data from the equatorial Indian Ocean during the CINDY/DYNAMO field program in late 2011. This period was special because the field program obtained a number of observations not routinely available; in particular, the sounding array it deployed allows estimation of the advection terms directly from observations. We complement this with satellite-based radiation observations and large-scale estimates of surface fluxes. Some results are shown in Fig. 3.

Extratropical variability and predictability. The new post-doc, Lei Wang, joined us in September 2013. He will implement an empirical prediction model for extratropical LFV to characterize intraseasonal predictability and its seasonal dependence.

Downscaling Weather and Seasonal Climate. We have assessed the probabilistic skill of the North American Multi-model Ensemble (NMME), and have shown that regression-based correction of climate forecasts using least-squares estimates are unreliable. Our extreme index methodology — developed initially for tropical cyclogenesis and later extended to tornado activity — has been applied to hail.

Sea Ice. We have conducted empirical orthogonal function (EOF) and multivariate EOF (mEOF) analysis on the Arctic sea ice concentration and associated atmospheric variables and developed a linear Markov model to predict the principal components. We discovered and reported a teleconnection
between late-fall sea ice in the Barents-Kara-Greenland Seas and early-winter sea ice in the Bering Sea.

RESULTS

Data-driven multilayered low-order stochastic models. The structure of the MSM equations, albeit nonlinear, is such that the dynamics of the unresolved variables is orthogonal to that of the resolved ones. Likewise, the EMR formalism decomposes the dynamics of the unresolved variables across several mutually orthogonal levels. Based on these features, we developed an EMR formulation with energy-conserving nonlinearities and applied it to an idealized, partially observed, nonlinear and stochastic climate model with fully coupled slow and fast variables. The resulting energy-conserving EMR model efficiently captures the main features of the stochastic dynamics of the slow variables, even when the correlation decay times of the resolved and unresolved variables are comparable.

Reduced Markov models with state-dependent noise, and Ruelle-Pollicott resonances. This result relies on appropriately representing the dynamics by Markov operators adapted to a given observable. Such operators correspond to Markov reduced models with state-dependent noise that reflects the statistics of the unobserved variables. We have shown the model statistics of an intermediate-complexity ENSO model become more sensitive to parameter changes as the spectral gaps of the associated Markov operator become smaller: small gaps correspond to regimes where peaks in the power spectrum are the most energetic, while correlations decay more slowly.

ENSO and coupled variability on seasonal time-scales. Figure 1 (left) shows the correlation between the NOAA OISST and CFSv2 predictions of Atlantic SST in the MDR for Jan. 1982–Dec. 2010; this panel is reproduced from Fig. 9 of Hu et al. (2013). Figure 1 (right) shows the same statistic for predictions from the new VAR model (Lee et al., in prep.). The statistical model, which uses only global SST data over the year preceding the forecast initial date, outperforms CFSv2, one of the better participants in NMME. Note that VAR is generally more skillful at longer leads. In particular, for the months of strongest hurricane activity (Aug.-Sept.-Oct.), VAR out-predicts CFSv2 and has a useful level of skill for eight or more months ahead.

Development of a low-order statistical MJO model. Kondrashov et al. (2013b) performed a PNF-based predictability study of the MJO and found that PNF considerably improves predictions of the MJO phase. Even when forecasts are initiated from weak MJO conditions, useful skill is maintained out to 30 days. PNF also significantly improves the skill for initial states associated with an MJO phase over the Indian Ocean.

Development of a low-order dynamical MJO model. The recent modifications in our model resulted in a new capability to simulate the MJO in a nonlinear framework, as an organic outgrowth of a tropical climate that contains longitudinal asymmetries. With a warm pool imposed by zonally varying ocean heat transport, we can now simulate persistent eastward-propagating disturbances in the presence of a reasonable mean state (Fig. 2). A still preliminary, but crucial scientific conclusion is that ocean coupling may play a role even when the SST anomalies are very small.

Analysis of MJO observations. Observational analysis supports our LDM and provides indications for its improvement. Variations in radiative heating are in phase with precipitation and MSE, and are larger than those in surface turbulent fluxes, which lag precipitation. Radiative cooling emerges as the dominant process driving MJO instability. Vertical advection acts to damp the MJO, consistent with a positive gross moist stability, as assumed in our model. Furthermore, recent analysis supports our
hypothesis that the MJO is a “moisture mode” in the Indian Ocean, but transitions to a more Kelvin wave-like disturbance as it crosses the Maritime Continent (Sobel and Kim, 2012).

**Extratropical variability and predictability.** We have carried out a preliminary study to determine the preferred region of summer heat wave activities in both the current climate and the future climate. In this study, we examined the monthly mean temperature variance in seven state-of-the-art coupled ocean-atmosphere models participating in CMIP5, along with data from the NCEP/NCAR reanalysis (Fig.4). The Eurasian continent as well as North America are regions of large variability in both models and observations, although the North American patterns differ between observations and models.

**Downscaling climate to weather extremes.** We have continued our use of a regression-based index to downscale tornado activity from atmospheric variables and have found interannual simulation skill on regional scales (Table 1). Preliminary results applying the methodology to hail are encouraging.

**Subseasonal to seasonal monsoon predictability of daily weather statistics.** Moron et al. (2012) related daily rainfall characteristics during the Indian summer monsoon to an interannually modulated annual cycle (MAC) and a 30–60-day intraseasonal oscillation (ISO). We have extended this work with the purpose of assessing the impact on rainfall of predictability inherent in these modes (manuscript in preparation). We have also explored three-way interactions between the Indian monsoon, the North Atlantic, and the tropical Pacific, showing that the individual records exhibit highly significant oscillatory modes with spectral peaks at 7–8 yr, as well as in the quasi-biennial and quasi-quadrennial bands (Feliks et al., 2013).

We have further quantified the role of the MJO and ENSO in subseasonal-to-seasonal predictability, by analyzing hindcasts from three global ensemble prediction systems (EPS). The results support the concept that “windows of opportunity” for high forecast skill do exist (manuscript in preparation). A multiscale-modeling framework for daily rainfall was applied to the winter season in Northwest India. Our findings help clarify the sequence of Northern Hemisphere mid-latitude storms bringing winter rainfall over Northwest India, and their association with potentially predictable low-frequency modes on seasonal time scales and longer (Pal et al., 2013).

**Sea ice.** EOF and mEOF analysis of Arctic sea ice concentration (Figs. 5 and 6) reveal spatially coherent patterns in the in the Baffin Bay and in the Barents, Kara and Greenland Seas, in the Atlantic sector of the Arctic, and in the Bering and Okhotsk Seas, in the Pacific sector. The dominant signal is the long-term declining trend in the Arctic basin. We developed a linear Markov model to predict the principal component of each mEOF mode that out-performs persistence, in particular at lead times longer than 2–4 months (Fig. 7). Sea ice thickness information contributes most to the hindcast skill, followed by SST and surface air temperature (Fig. 7). Moreover, during winter and spring, most of the hindcast skill comes from marginal sea ice, particularly in the Atlantic sector of the Arctic, while the central Arctic basin is more predictable during summer and fall (Fig. 8). Sea ice concentration in the Atlantic sector is much more predictable than in the Pacific sector (Figs. 7 and 8).

A teleconnection between late fall sea ice in the Barents-Kara-Greenland Seas and early-winter sea ice in the Bering Sea is facilitated by an atmospheric Rossby wave generated by a fall sea ice anomaly in the former. It is this anomaly that creates anomalous cold advection near the Bering Sea in early winter. This teleconnection was robust in the 1980s and 1990s, but it broke down after 1998, when sea ice reduction in the Barents-Kara-Greenland Seas started to accelerate (Yang and Yuan, 2013).
**IMPACT/APPLICATIONS**

**RELATED PROJECTS**

*Methodological developments.* The work on the EMR and MSM methodology carried out under ONR-MURI funding is complemented by work performed with NSF-DMS–led support in the framework of an NSF-DOE-DOA program on Earth System Modeling. The latter work, under the same Lead PI, concentrates on climate sensitivity; it involves two other universities besides UCLA, namely Indiana University and the University of Nevada, Reno, as well as additional Co-PIs at UCLA. The present work concentrates on prediction and the two projects benefit strongly from each other, including the joint support of a post-doc (Honghu Liu).

*MJO.* The work described herein is complementary with two of our other projects. One project, funded by the NASA Modeling and Analysis Program, involves simulation of the MJO in the NASA GISS climate model. Another, funded by the NSF Large-Scale Dynamics program, involves cloud-resolving simulation of the MJO. The present project is distinct from those two in its explicit focus on development of a low-order model, as opposed to simulation with comprehensive “full-physics” models (GCM for NASA, CRM for NSF).

*Extratropical variability and predictability.* We also examined intensity and position changes of subtropical highs during northern summer in 20th-century observations and in 21st-century model simulations (Li et al., 2012). We found that the enhancement of subtropical highs, which can contribute to the increase in LFV of surface temperatures, is likely to be caused by enhanced land-ocean heat contrasts in the future. In another related study, we examined near-term changes in Southwestern United States hydroclimate and the mechanisms that may lead to these changes (Seager et al., 2013).

*Downscaling Weather and Seasonal Climate.* Our work on tornado and severe weather downscaling is also supported by a Research Initiative in Science and Engineering Award from Columbia University, on “Towards Long-Range Prediction of Tornado Activity.”

**REFERENCES**


PUBLICATIONS


**HONORS/AWARDS/PRIZES**

- Mark Cane, Columbia University, Elected, National Academy of Sciences, 2013.
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Table 1: Correlation between the index and reported number of tornadoes by U.S. climate region and month for the period 1979-2010. Significant correlations are in bold font. Regions and months with less than 32 reported tornadoes during the period are omitted.